

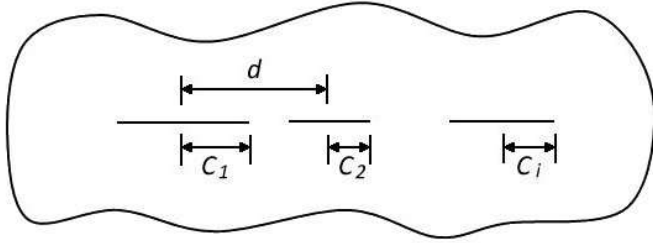
# AFGROW Workshop 2022

## Multisite Damage Solution

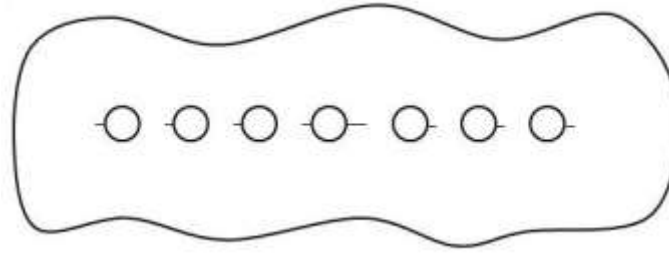
James Harter, Alexander Litvinov

LexTech, Inc .

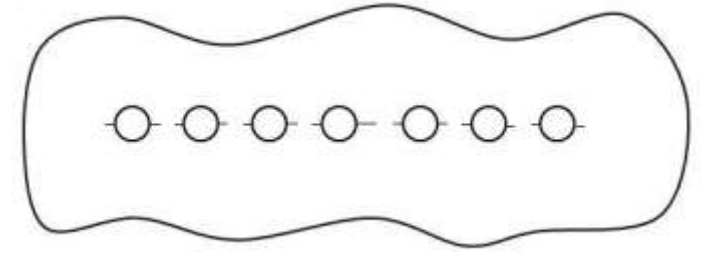
# Through Crack Cases (Infinite Plate)



Multiple Through Cracks



Multiple Holes, Continuing Damage



Multiple Holes, Full MSD Scenario



AFRL-RQ-WP-TR-2014-0233

**IMPROVED STRESS INTENSITY SOLUTIONS  
DEVELOPED FOR THE MULTIPLE SITE DAMAGE  
SCENARIO**

**Two Unequal Through Cracks on Either Side of an Open Hole,  
Multiple Through Cracks, and Through Cracks Approaching an Open  
Hole**

**James A. Harter**

**Structures Technology Branch  
Aerospace Vehicles Division**

**OCTOBER 2014  
Interim Report**

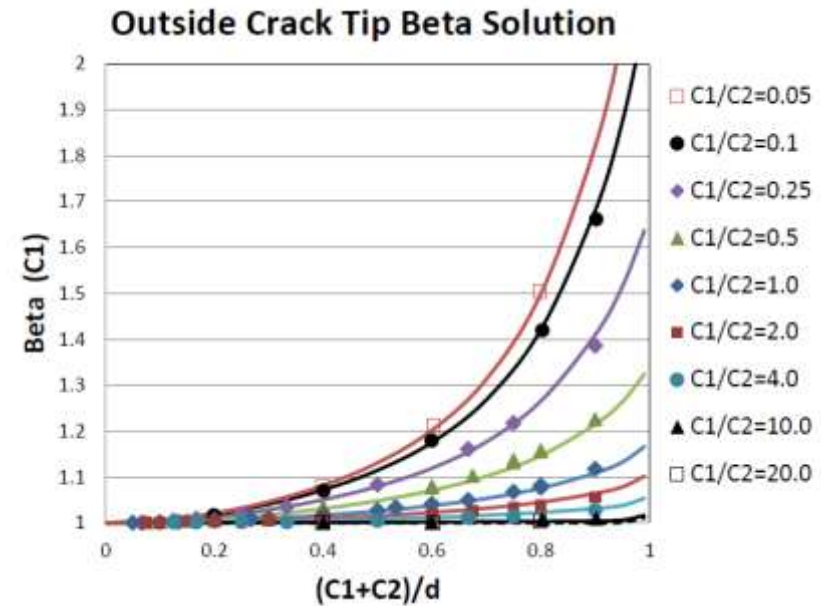
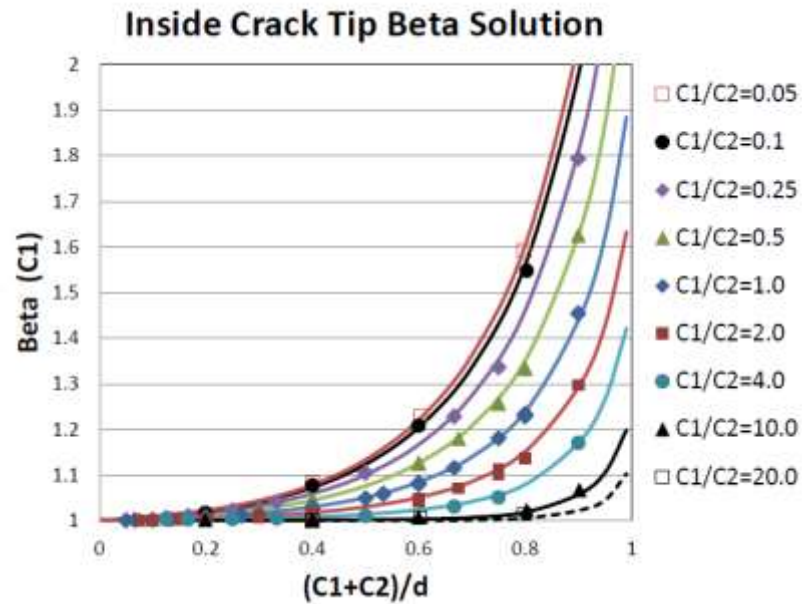
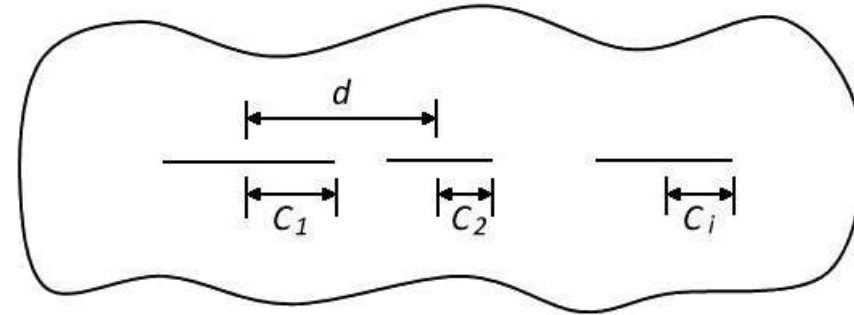
**Approved for public release; distribution unlimited.**

*See additional restrictions described on inside pages*

# Multiple Through Crack Case

First, consider the two-crack case

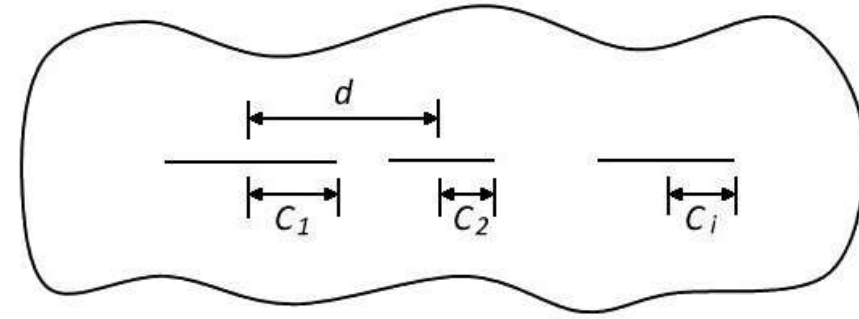
Four crack tips (2 inside crack tips and 2 outside crack tips)  
Two Parameters:  $C_1/C_2$ , and  $(C_1 + C_2)/d$



Curve fit solutions available in the baseline reference

# Multiple Through Crack Case Solution Procedure

- To solve for any number of through cracks, consider the crack of interest to be  $C_1$  and calculate the beta value for each crack tip using the appropriate curve fit equation for each crack from 2 through  $i$  (total number of cracks).
- The inside crack tip is toward the adjacent crack and the outside crack tip is on the opposite side of the adjacent crack.
- AFGROW will allow  $3 \leq i \leq 9$  since the two-crack solution is available in the Advanced Interface
- The method of compounding is used to calculate the final beta solution for each crack tip.  $\text{Beta}_{\text{total}} = \text{Beta}_1 * \text{Beta}_2 * \dots * \text{Beta}_{(i-1)}$



The curve fit solution is very good for each compounded case, but since the error is also compounded, it can increase somewhat as the number of cracks increase. However, this is mitigated since the distance between cracks also increases so that the solution for several compounded cases will eventually converge toward 1.0. Typical error will be < 3%

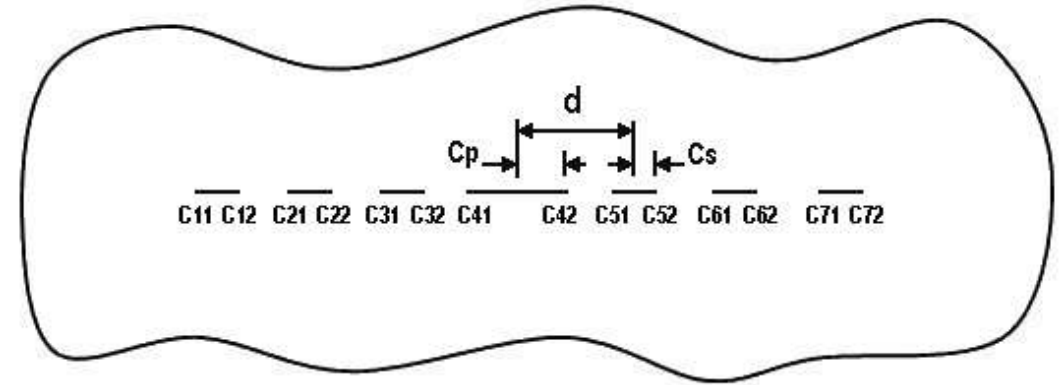
# Multiple Through Crack Case FEM Validation

Width	Spacing	Cp	Cs
75	0.5	0.1	0.05

Width	Spacing	Cp	Cs
150	1	0.1	0.05

	K	Beta	Eqn Beta	% Diff
C11	0.3991	1.006982	1.01012	0.3116
C12	0.3998	1.008748	1.02192	1.3057
C21	0.4027	1.016065	1.02043	0.4296
C22	0.4029	1.01657	1.02781	1.1057
C31	0.4074	1.027924	1.03343	0.5356
C32	0.4088	1.031457	1.03941	0.7711
C41	0.5687	1.014631	1.02394	0.9174
C42	0.5687	1.014631	1.02394	0.9174
C51	0.4088	1.031457	1.03941	0.7711
C52	0.4074	1.027924	1.03343	0.5356
C61	0.4029	1.01657	1.02781	1.1057
C62	0.4027	1.016065	1.02043	0.4296
C71	0.3998	1.008748	1.02192	1.3057
C72	0.3991	1.006982	1.01012	0.3116

K	Beta	Eqn Beta	% Diff
0.3963	0.999917	1.00336	0.3443
0.3965	1.000422	1.00993	0.9504
0.3978	1.003702	1.00735	0.3634
0.3978	1.003702	1.01167	0.7938
0.399	1.00673	1.01148	0.4718
0.3991	1.006982	1.01448	0.7446
0.5623	1.003213	1.00841	0.5180
0.5623	1.003213	1.00841	0.5180
0.3991	1.006982	1.01448	0.7446
0.399	1.00673	1.01148	0.4718
0.3978	1.003702	1.01167	0.7938
0.3978	1.003702	1.00735	0.3634
0.3965	1.000422	1.00993	0.9504
0.3963	0.999917	1.0036	0.3683



FEM width set as  $150 * d$  to approximate an infinite plate

# Multiple Cracked Holes

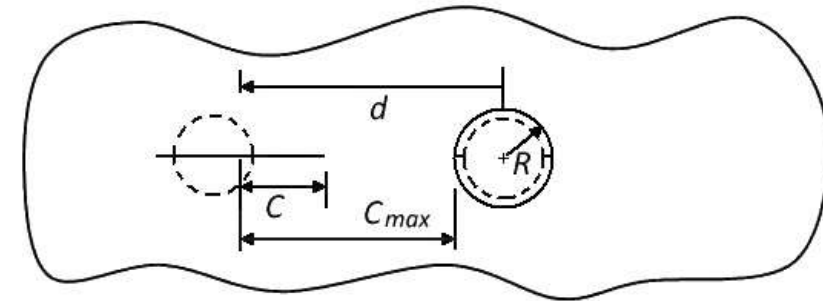
## Axial Load Case

We use the current AFGROW Advanced Model solution for two unequal through cracks at a hole and apply corrections for cracked, adjacent holes using the method of compounding.

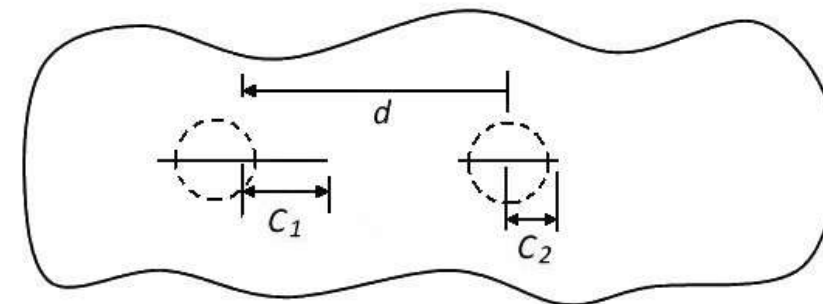
### Two Possible Corrections

If the crack(s) at an adjacent hole are small ( $\leq R/3$ ), then we use the correction from the baseline reference for a through crack approaching a hole.

If the crack(s) at an adjacent hole are larger ( $> R/3$ ), we use the correction for a crack approaching another crack. This correction was explained in previous slides.

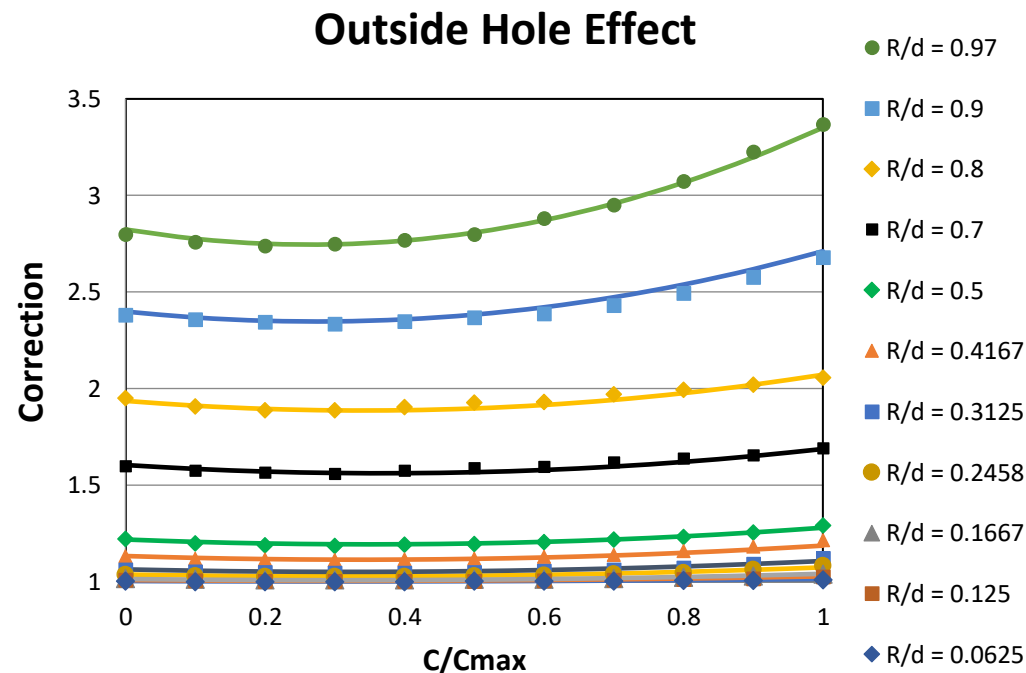
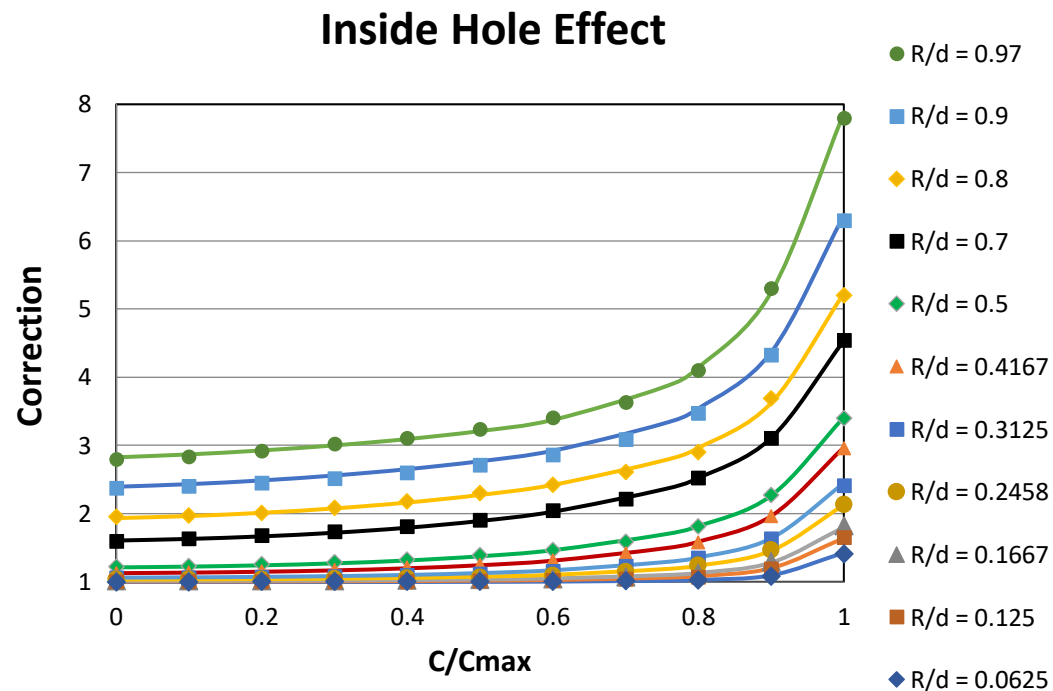


Crack Approaching a Hole



Crack Approaching a Crack

# Through Crack Approaching a Hole Correction

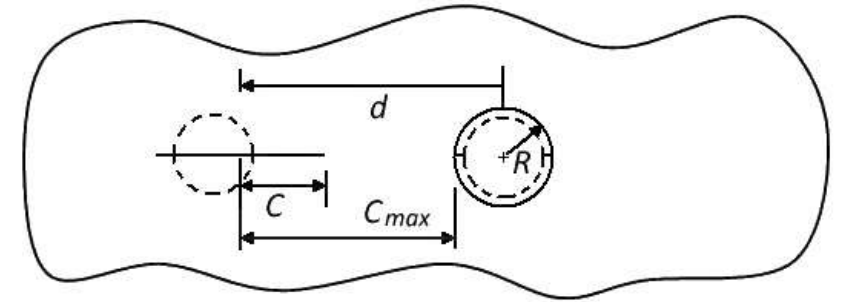


Curve fit solutions available in the baseline reference

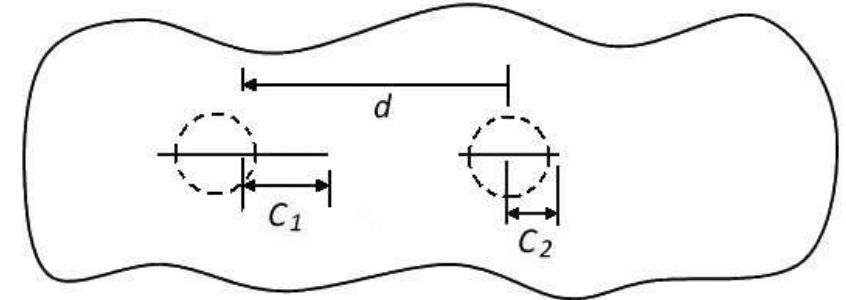


# Multiple Cracked Holes Solution Procedure

- To solve for any number of holes, start from the hole of interest, calculate the beta solution for a given crack tip using the Advanced Model Solution for one or two non-symmetric cracks with no adjacent holes. Calculate the beta correction value for each adjacent cracked hole using the appropriate correction model for each hole from 3 through  $i$  (total number of holes).
- The inside crack tip is toward the adjacent hole and the outside crack tip is on the opposite side of the adjacent hole.
- AFGROW will allow  $3 \leq i \leq 9$  (odd number)
- The method of compounding is used to calculate the final beta correction for each crack tip.  $\text{Correction}_{\text{total}} = \text{Correction}_1 * \text{Correction}_2 * \dots * \text{Correction}_{(i-1)}$



Crack Approaching a Hole



Crack Approaching a Crack

# Multiple Cracked Holes FEM Validation

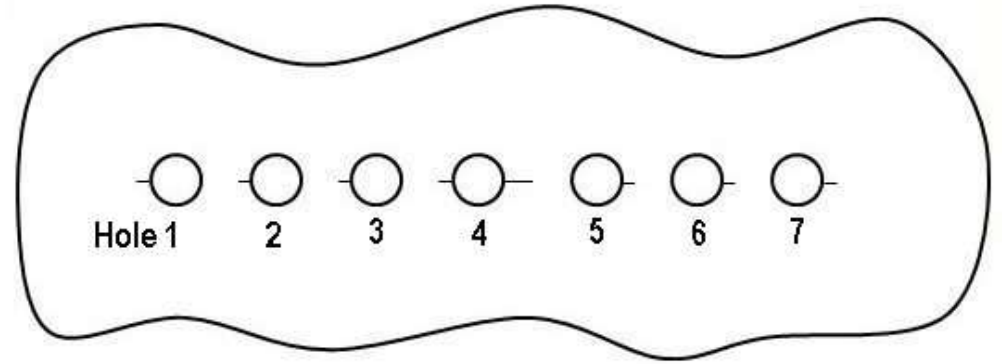
Hole Dia.	Spacing	Pin Load	ByPass	Thickness	Width	Height
0.25	4D	0	10	0.04	50	250

Cp	Cs
0.05	0.005

Stress Intensity								
	Hole 1	Hole 2	Hole 3	Hole 4		Hole 5	Hole 6	Hole 7
<b>K</b>	3.165	3.201	3.213	3.291	7.228	3.215	3.201	3.165
Beta								
<b>Beta</b>	2.525	2.554	2.564	2.626	1.824	2.565	2.554	2.525
<b>Equation</b>	2.494	2.517	2.521	2.624	1.784	2.521	2.516	2.494
<b>Diff (%)</b>	-1.231	-1.466	-1.645	-0.084	-2.202	-1.715	-1.474	-1.234

Cp	Cs
0.25	0.1

Stress Intensity								
	Hole 1	Hole 2	Hole 3	Hole 4		Hole 5	Hole 6	Hole 7
<b>K</b>	8.080	8.270	8.401	10.380	10.410	8.495	8.284	8.084
Beta								
<b>Beta</b>	1.442	1.475	1.499	1.852	1.175	1.516	1.478	1.442
<b>Equation</b>	1.406	1.440	1.466	1.849	1.183	1.480	1.442	1.407
<b>Diff (%)</b>	-2.471	-2.376	-2.221	-0.154	0.670	-2.380	-2.413	-2.479



# Bearing Load Effect

# Bearing Load Effect on Adjacent Holes

Width (in)	Total Height (in)	Thickness (in)	Hole Dia (in)	Spacing (hole dia)	ByPass (Ksi)	Pin Load (Kip)	Fastener Material
50	250	0.04	0.25	4	10	0.2	Steel

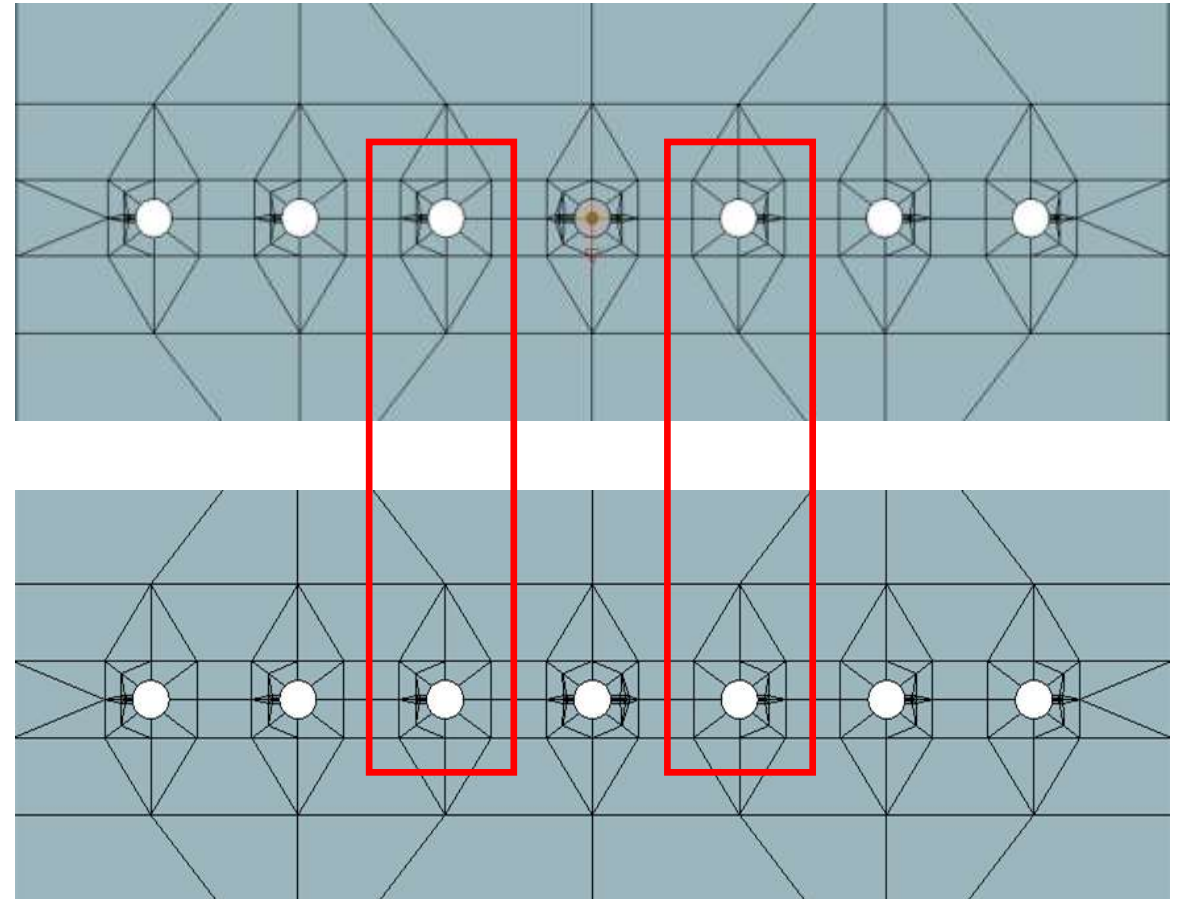
Pin Load in Center Hole Only			
Cp	Cs	Kp	Ks
0.1	0.05	10.96	11.16

Adjacent Holes	
K Left	K Right
7.819	7.832



No Bearing Load (all open holes)			
Cp	Cs	Kp	Ks
0.1	0.05	8.562	8.46

Adjacent Holes	
K Left	K Right
7.652	7.661



# New Bearing Load Solution for Multiple Holes

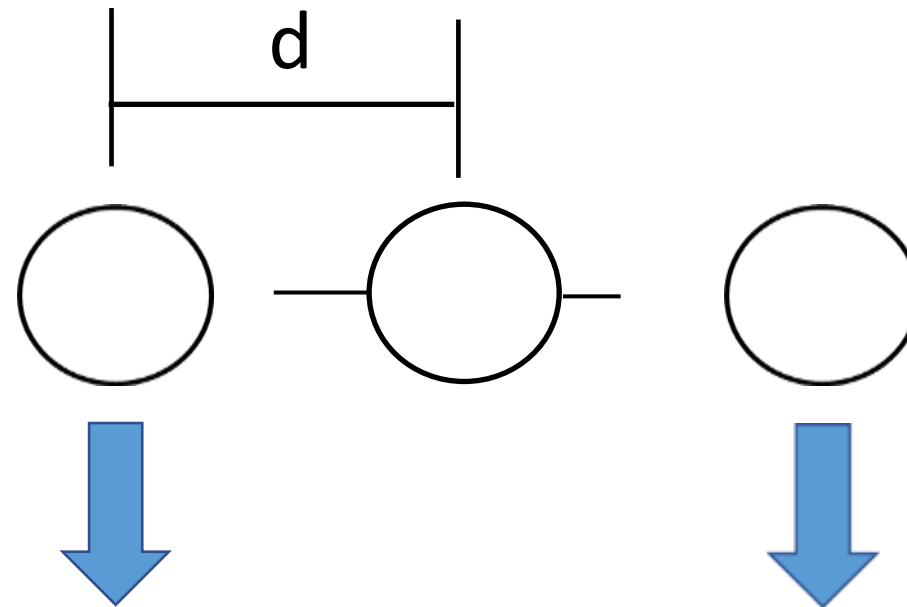
We have developed a bearing solution for the multiple hole geometry that accounts for the following effects:

- Different bearing loads at each hole
- Influence of bearing load on adjacent holes

This solution is currently being validated and we plan to include it in our upcoming new release.

# Effect of Adjacent Pin Loaded Holes

Multiple FE runs were used to develop an algorithm to account for the adjacent pin loading for the adjacent holes as a function of hole spacing



# Multiple Cracked Holes

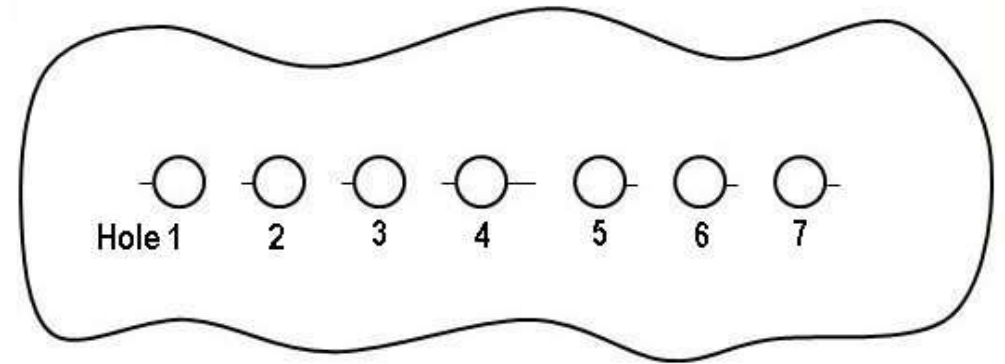
## FEM Validation

Hole Dia.	Spacing	Pin Load	ByPass	Thickness	Width	Height
0.25	4D	0.4	10	0.04	50	250

	Cp	Cs	Stress Intensity					
	0.05	0.005						
	Hole 1	Hole 2	Hole 3	Hole 4	Hole 5	Hole 6	Hole 7	
K	8.433	8.418	8.341	8.602	13.87	8.358	8.422	8.435
Equation	7.758	7.855	7.901	8.246	14.412	7.908	7.856	7.758
Diff (%)	-8.003	-6.684	-5.275	-4.143	3.909	-5.390	-6.718	-8.022

	Cp	Cs	Stress Intensity					
	0.075	0.025						
	Hole 1	Hole 2	Hole 3	Hole 4	Hole 5	Hole 6	Hole 7	
K	12.830	12.980	12.980	13.930	14.360	13.000	12.990	12.830
Equation	12.842	13.028	13.121	14.312	14.725	13.137	13.030	12.843
Diff (%)	0.096	0.367	1.089	2.745	2.540	1.050	0.306	0.101

	Cp	Cs	Stress Intensity					
	0.1	0.05						
	Hole 1	Hole 2	Hole 3	Hole 4	Hole 5	Hole 6	Hole 7	
K	13.710	14.000	14.070	15.570	14.880	14.090	14.000	13.710
Equation	14.183	14.425	14.552	16.161	15.228	14.573	14.428	14.184
Diff (%)	3.453	3.036	3.426	3.794	2.339	3.429	3.057	3.460

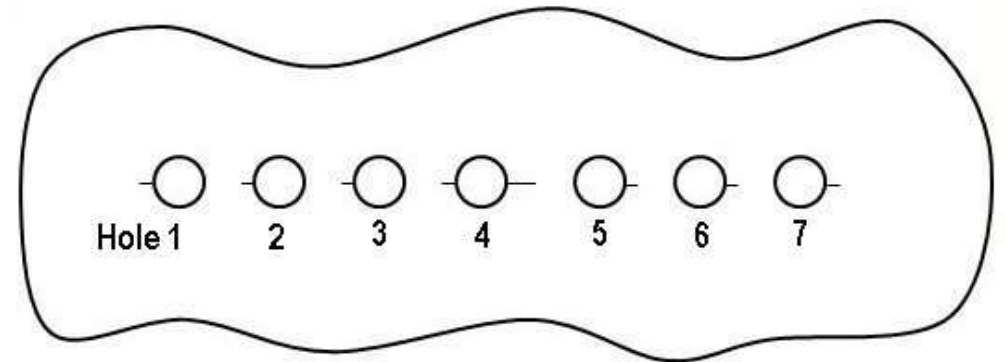


	Cp	Cs	Stress Intensity					
	0.25	0.1						
	Hole 1	Hole 2	Hole 3	Hole 4	Hole 5	Hole 6	Hole 7	
K	13.850	14.360	14.600	18.240	16.030	14.750	14.380	13.860
Equation	14.451	14.806	15.064	18.711	16.511	15.208	14.825	14.457
Diff (%)	4.341	3.103	3.177	2.580	2.999	3.103	3.094	4.309

# Multiple Cracked Holes FEM Validation

		Hole 4	Other Holes				
Hole Dia.	Spacing	Pin Load	Pin Load	ByPass	Thickness	Width	Height
0.25	3D	0.5	0.25	10	0.04	50	250

		Cp	Cs					
		0.1	0.05					
		Stress Intensity						
	Hole 1	Hole 2	Hole 3	Hole 4	Hole 5	Hole 6	Hole 7	
K	11.690	12.230	12.530	17.560	16.670	12.590	12.240	11.700
Equation	11.872	12.223	12.915	17.884	16.638	12.977	12.228	11.874
Diff (%)	1.559	-0.057	3.070	1.844	-0.195	3.076	-0.097	1.483

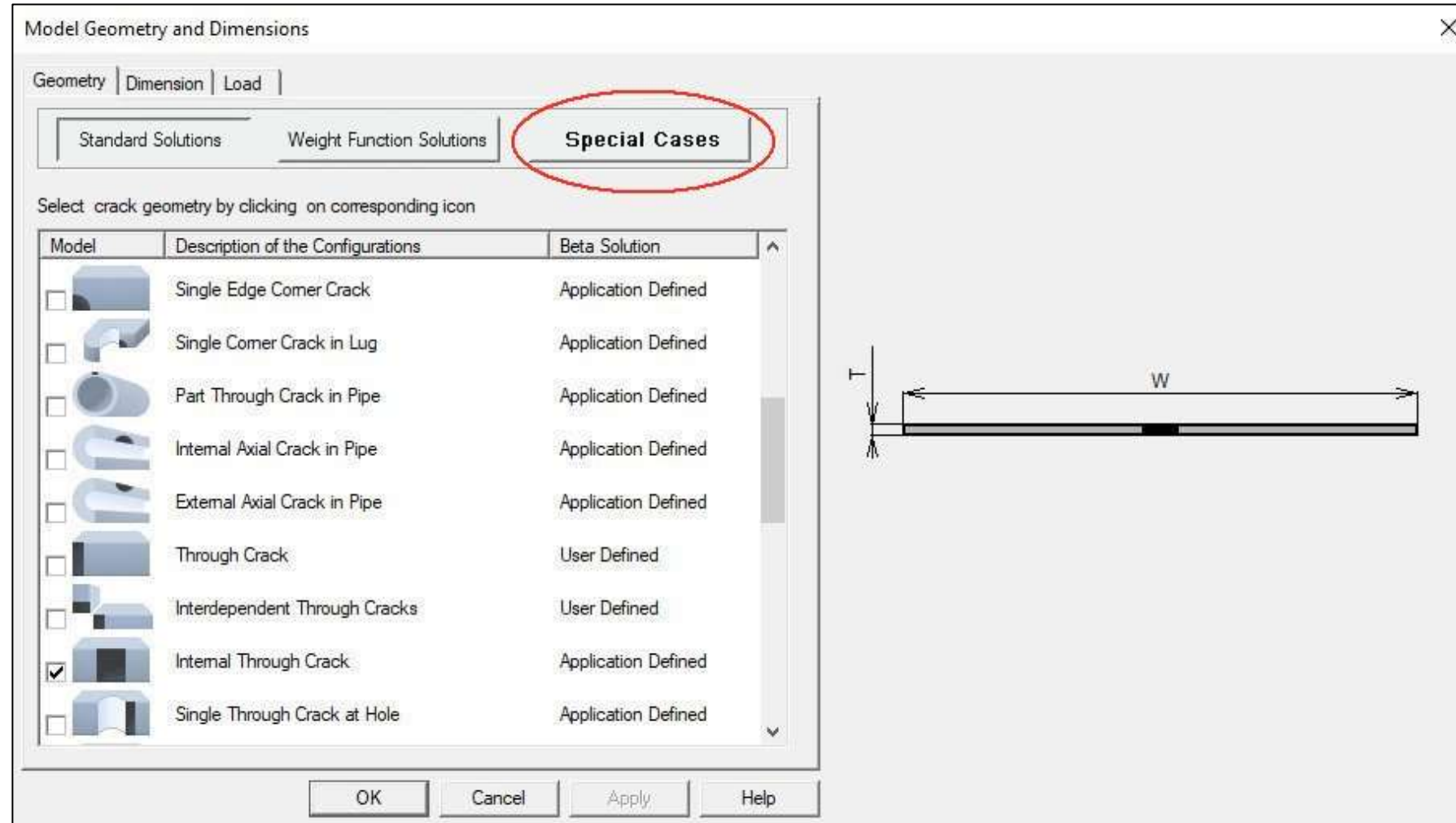


		Hole 4	Other Holes				
Hole Dia.	Spacing	Pin Load	Pin Load	ByPass	Thickness	Width	Height
0.25	6D	0.5	0.25	10	0.04	50	250

		Cp	Cs					
		0.1	0.05					
		Stress Intensity						
	Hole 1	Hole 2	Hole 3	Hole 4	Hole 5	Hole 6	Hole 7	
K	10.950	11.030	11.110	16.250	15.230	11.120	11.030	10.950
Equation	11.165	11.230	11.513	16.636	15.369	11.517	11.231	11.165
Diff (%)	1.965	1.815	3.624	2.376	0.911	3.574	1.820	1.966



# Implementation



# Proposed Special Cases

## **Multiple Through Cracks in an Infinite Plate**

- Axial load case
- 3 to 7 cracks

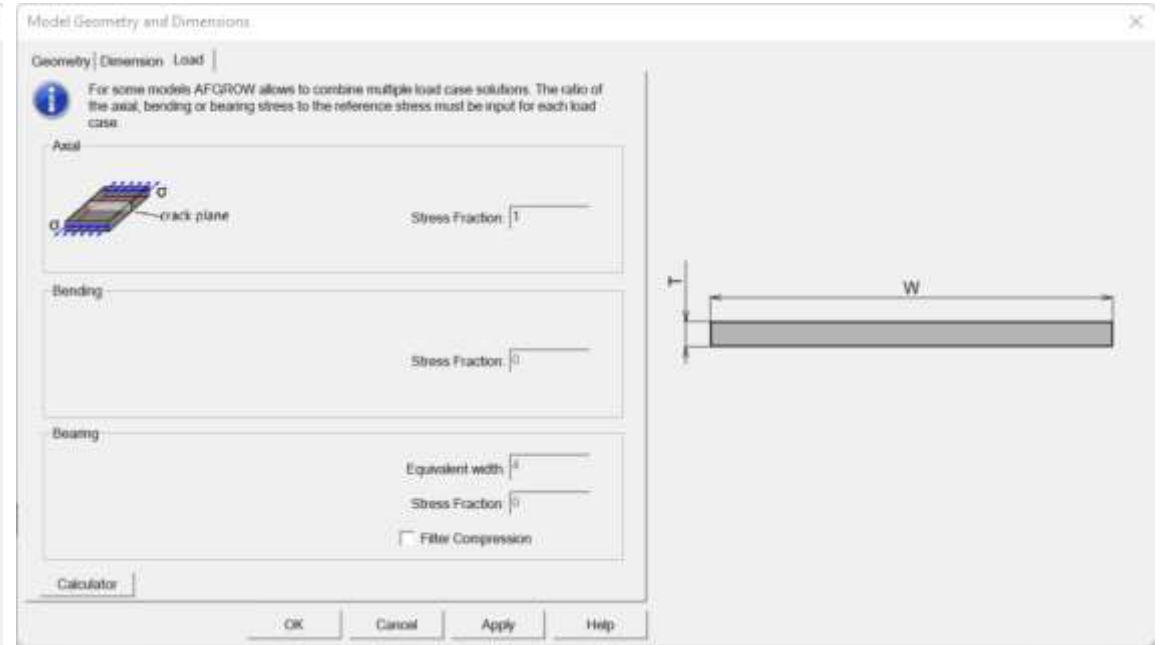
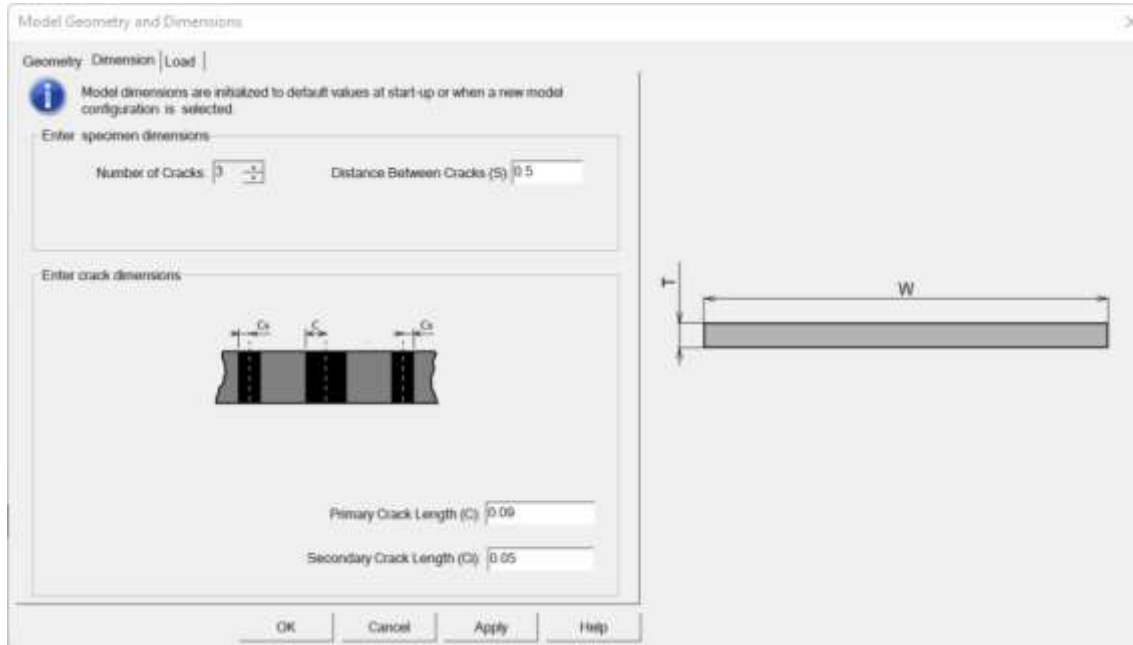
A secondary crack is added on each side of the model to simulate an infinite plate condition for all cracks in the model

## **Multiple Through Cracked Holes in an Infinite Plate (Continuing Damage)**

- Axial and bearing load cases
- Primary and Secondary Crack at the Center Hole
- Single Secondary Crack on Outside of each adjacent hole (2, 4, or 6 holes)

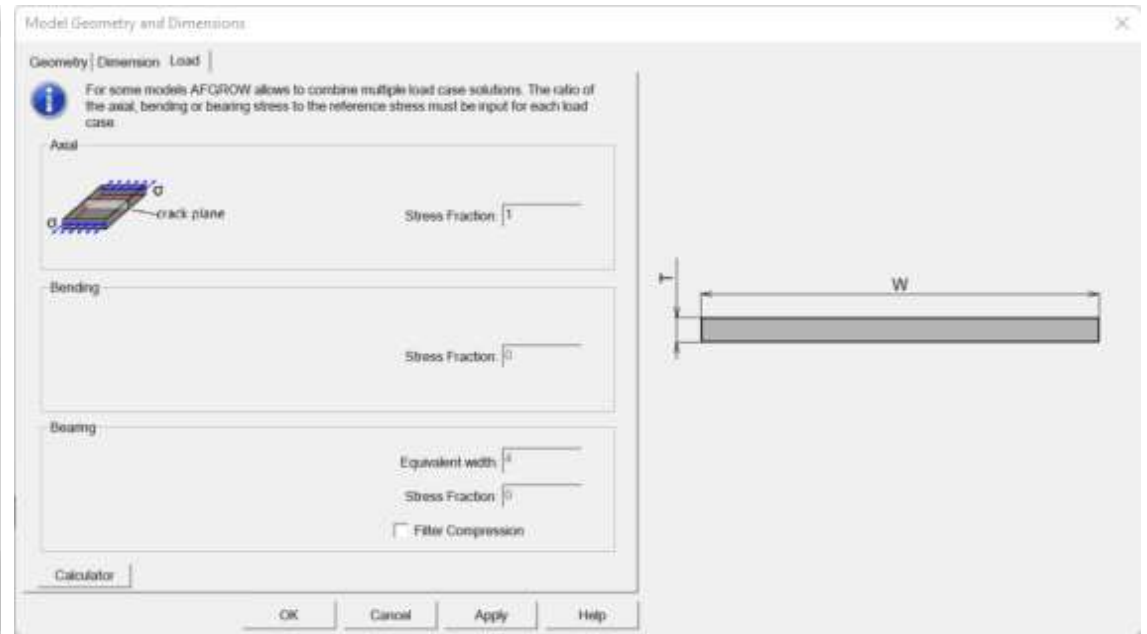
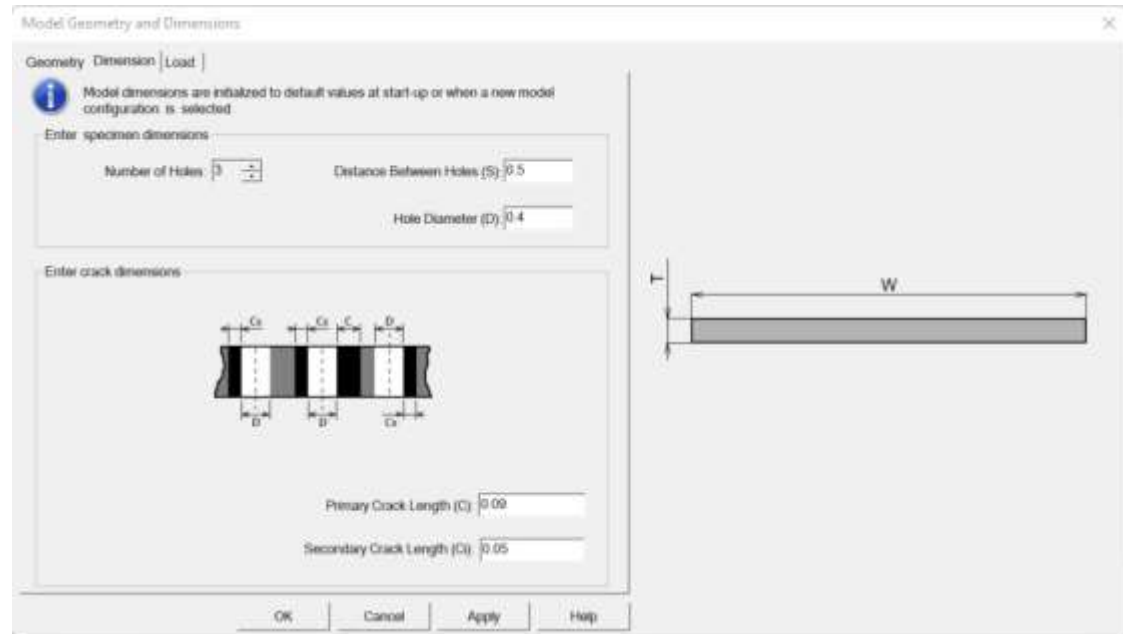
A secondary cracked hole is added on each side of the model to simulate an infinite plate condition for all cracks in the model

# Multiple Through Cracks



# Multiple Holes

Will Allow combinations of Axial, Bending, and Bearing Loading



# Questions/Comments?