



Through the Tensile Field.. An Investigation on the Residual Stress Field of a Cold Worked Hole

AFGROW Users' Conference

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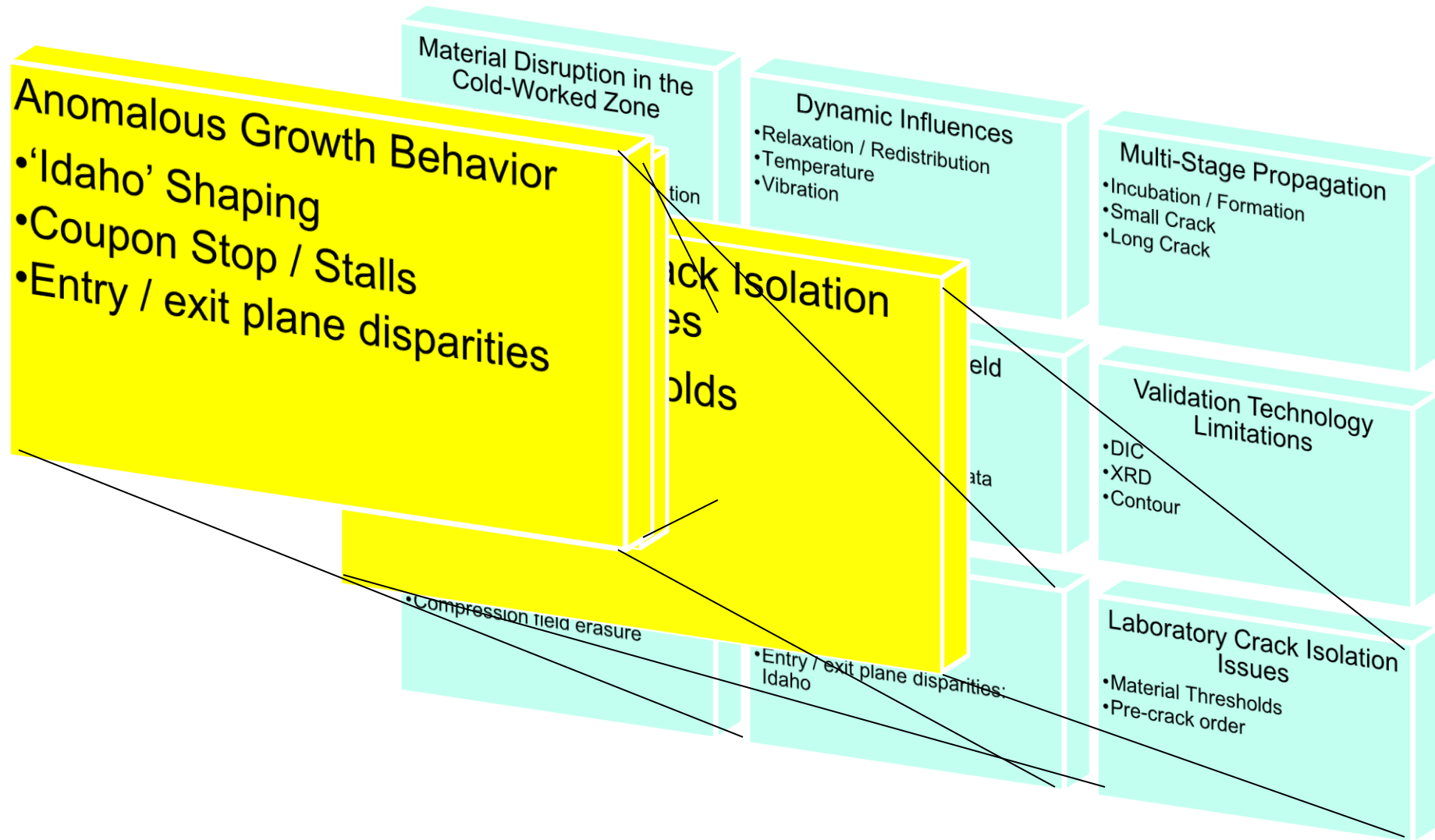
The Outline



*The Rationale to Reverse
Characterization Data and Beta Solutions
Fatigue Life Results
Residual 'K' Results*



Motivation: The Cold-Working Risk Matrix

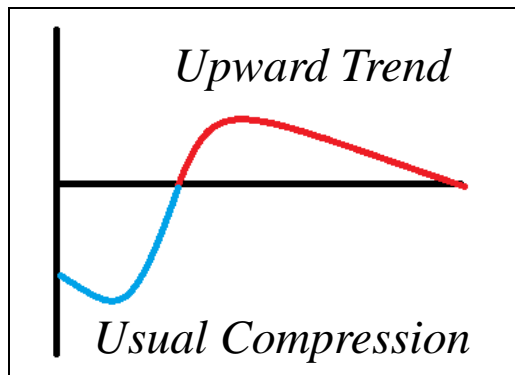
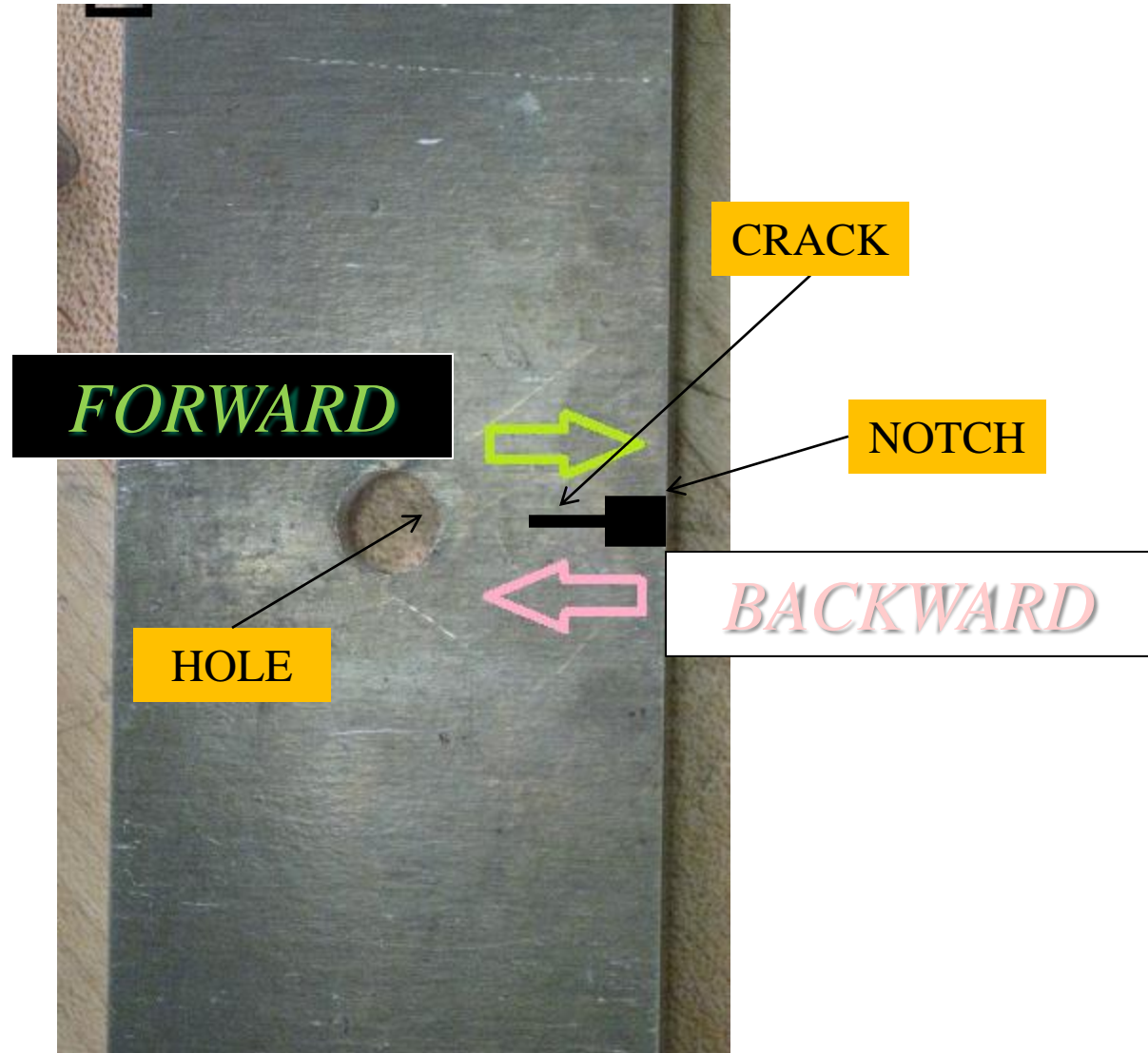




The Motivation & Terminology

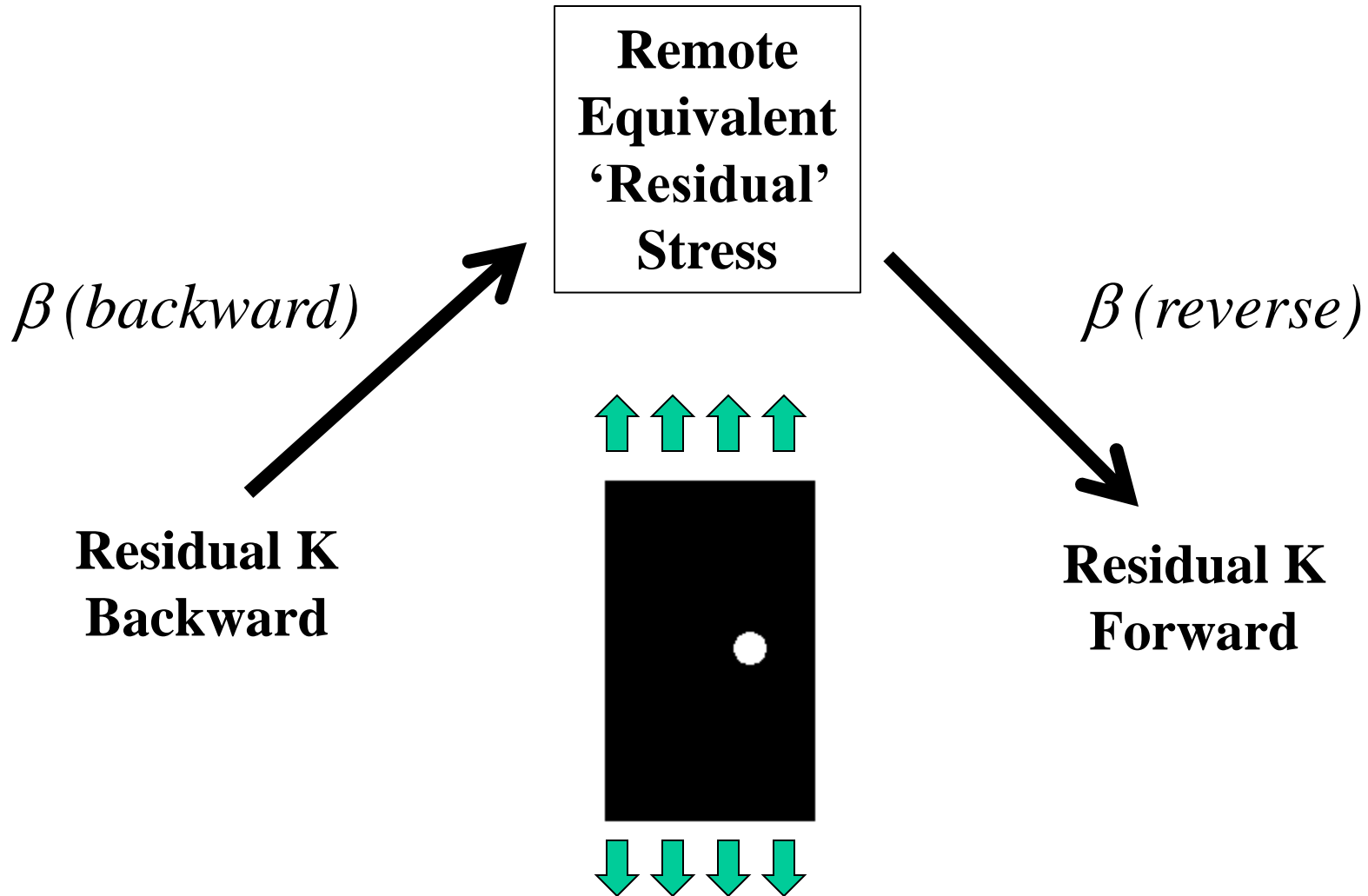


Hypothesis: *The residual stress of a cold-worked hole can be verified by growing a crack through the C_x field backwards then by reversing the geometry solution to generate a residual 'K' parameter*





Reversing the Residual Stress

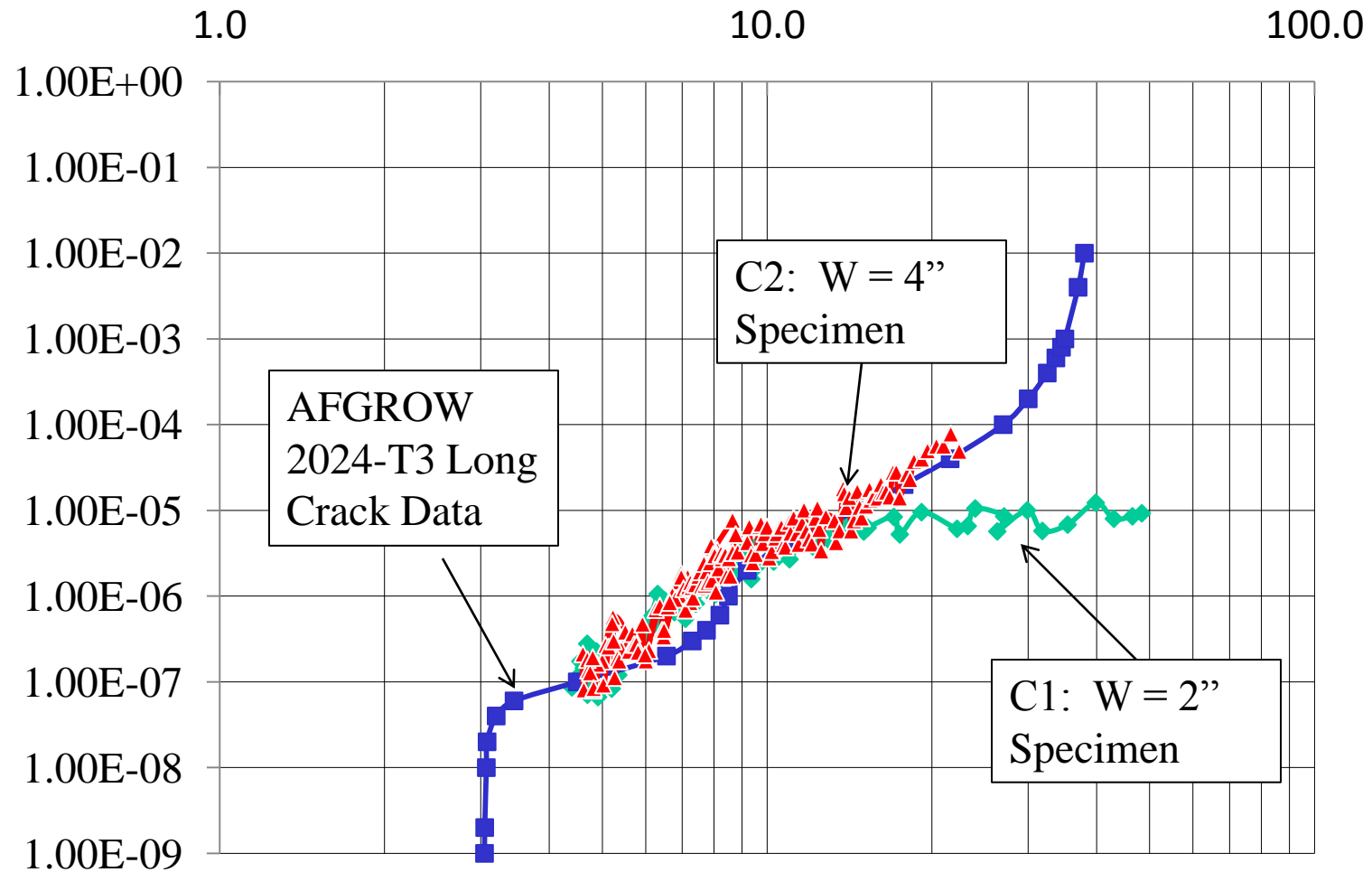




Characterization Results: Al-2024-T351 (Al-Clad)



da/dN (in / cycle) vs ΔK (ksi*sqrt(in))





Beta Solutions: AFGROW®



BACKWARD, 1.5
 $y = 496.22x^4 - 243.78x^3 + 45.777x^2 - 0.1196x + 1.1412$
 $R^2 = 0.9982$

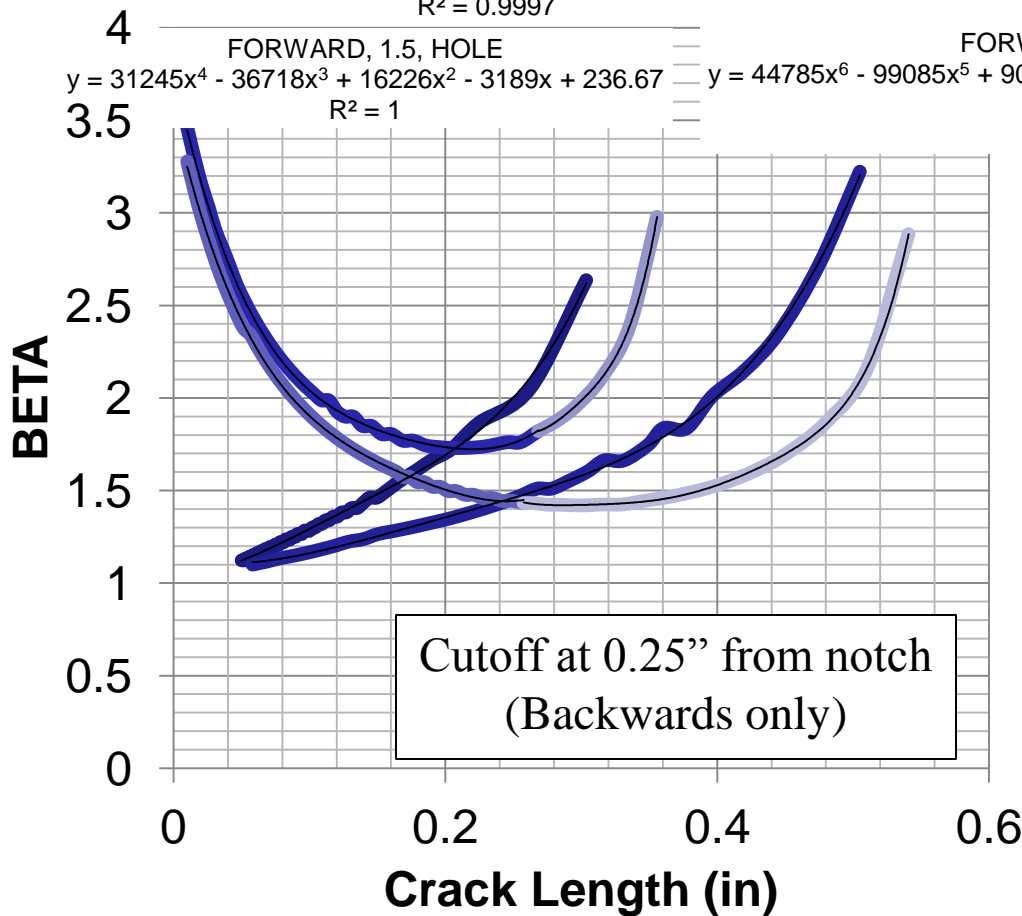
BACKWARD, 2.0
 $y = 130.07x^4 - 101.74x^3 + 30.09x^2 - 1.9188x + 1.1412$
 $R^2 = 0.9987$

FORWARD, 1.5, NOTCH
 $y = 1280.3x^4 - 891.7x^3 + 248.93x^2 - 34.546x + 3.7704$
 $R^2 = 0.9997$

FORWARD, 2.0, NOTCH
 $y = 1219.8x^4 - 836.37x^3 + 227.71x^2 - 32.093x + 3.5514$
 $R^2 = 0.9995$

FORWARD, 1.5, HOLE
 $y = 31245x^4 - 36718x^3 + 16226x^2 - 3189x + 236.67$
 $R^2 = 1$

FORWARD, 2.0, HOLE
 $y = 44785x^6 - 99085x^5 + 90565x^4 - 43730x^3 + 11767x^2 - 1674.1x + 99.861$
 $R^2 = 0.9999$



- backward, 1.5
- backward, 2.0
- forward, 1.5, notch
- forward, 2.0, notch
- forward, 1.5, hole
- forward, 2.0, hole
- Poly. (backward, 1.5)
- Poly. (backward, 2.0)
- Poly. (forward, 1.5, notch)

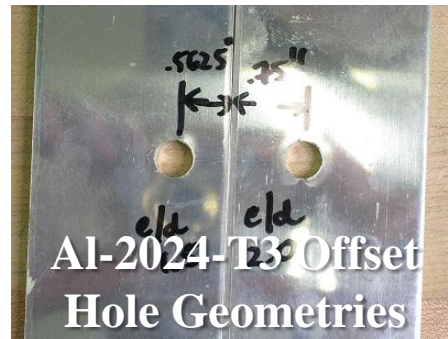
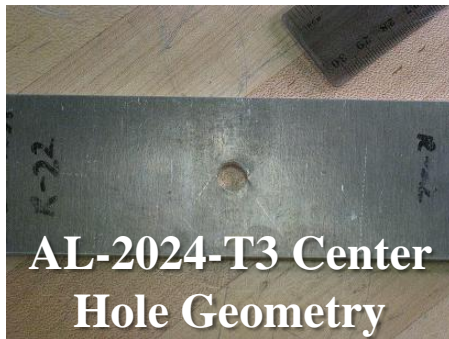


Testing Information



- Loading:
 - 15 ksi, $R = 0.0$
 - Constant Amplitude & “Constant K (Test)”
- Al-2024-T3 (Al-Clad), 1/8”, $e/d = 1.5, 2$
- 3/8” Hole (FTI:CBM-12-N-1-40-V1)

Constant Growth Rate !!!



IN PROGRESS



Results from Test Data



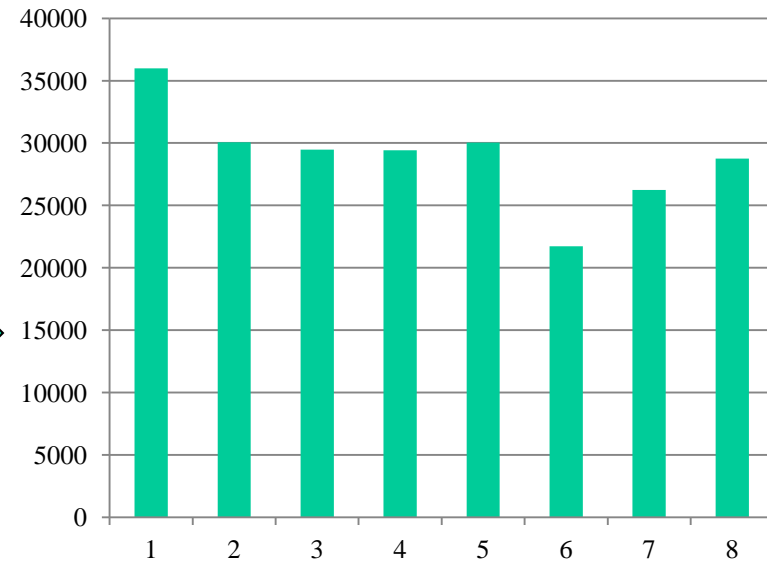
<i>Notch</i>	<i>Init. to ~0.15"</i>	<i>Crack Growth (CG)</i>		<i>Cont. Damage Init. & Failure</i>
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- More predictable results:
 - *CG Life* of cold worked hole < *CG Life* of the baseline
 - *CG Life* of 1.5 < *CG Life* of 2.0 (Baseline & Cx)
- Less obvious result:
 - *Total Life of Each Coupon is ~ Equal!*

TOTAL CYCLES
TO FAILURE



*Anonymous & Assorted
Constant Amplitude Results
($e/d = 1.5$ & 2.0)*



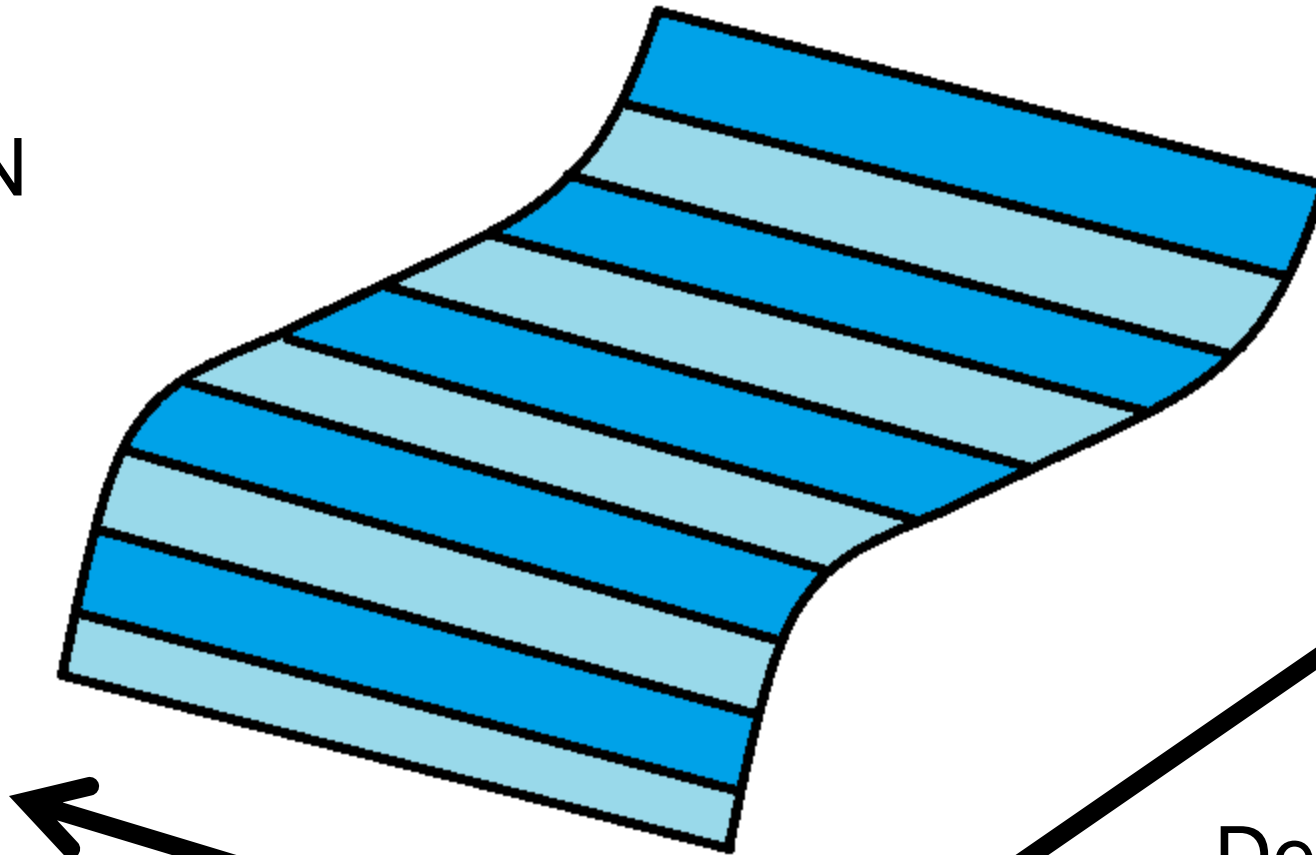
SAMPLE



Our FCG Curve in 3-Space



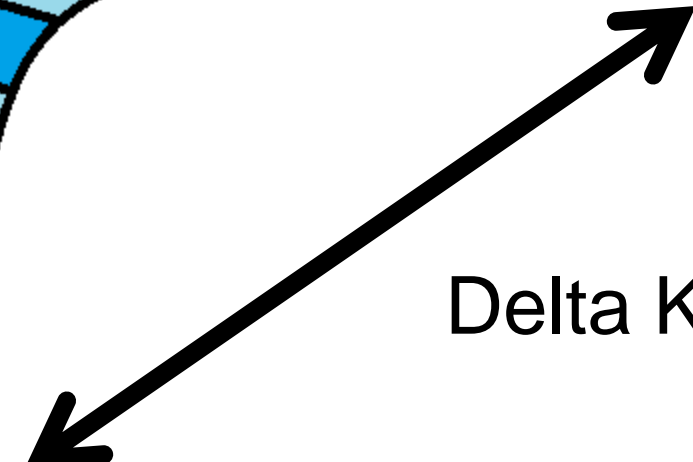
da/dN



R

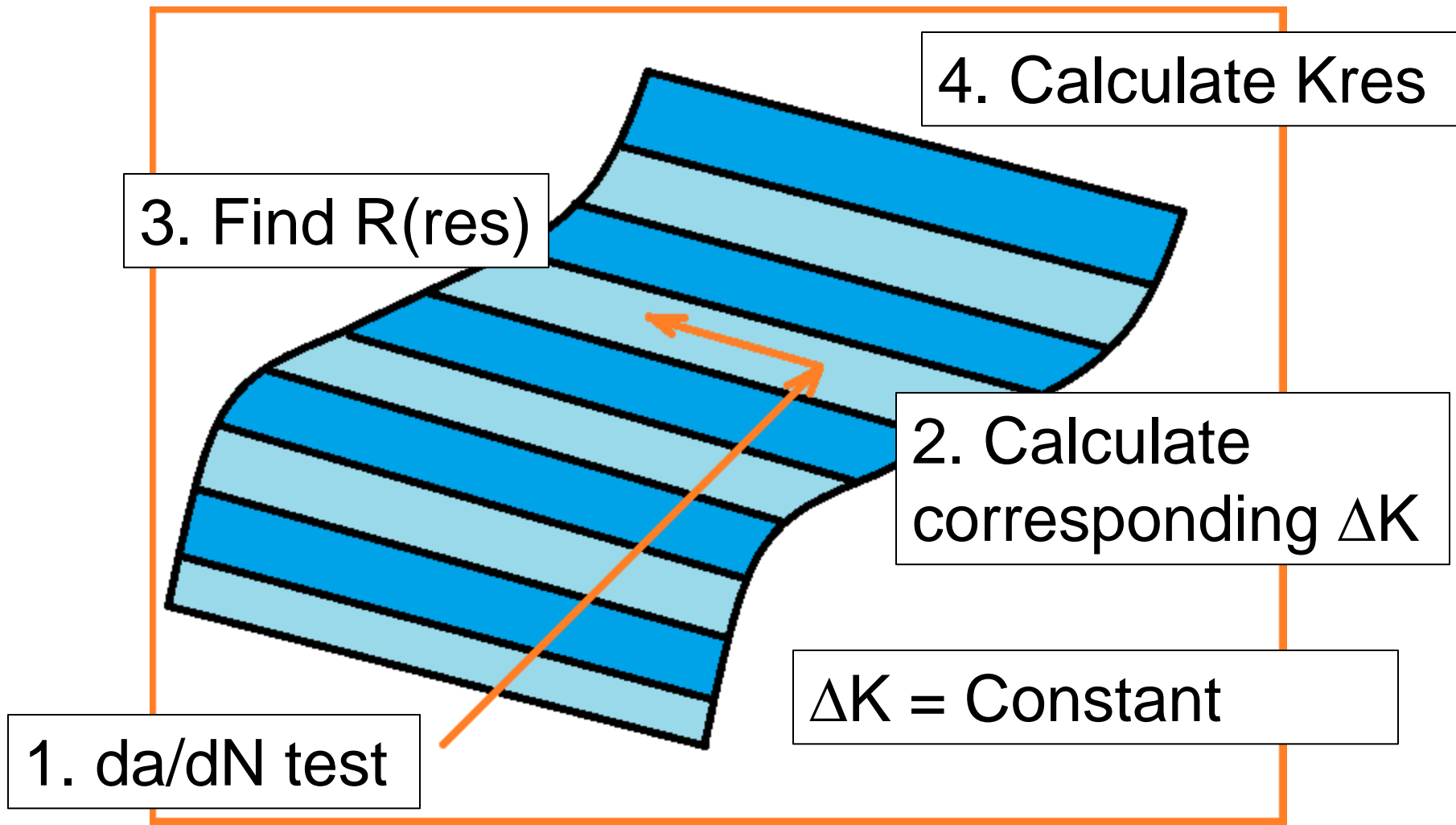


Delta K





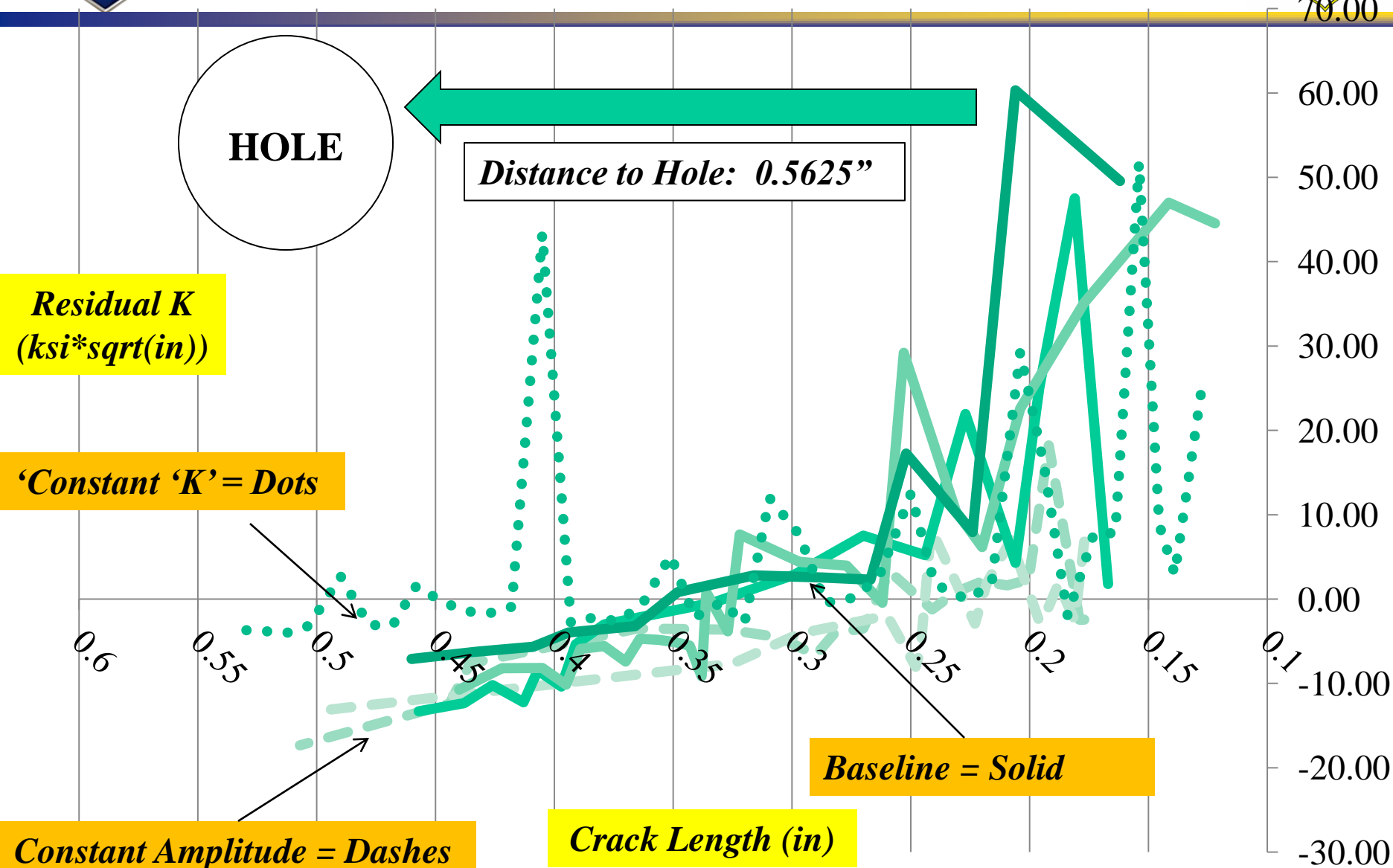
'Classic' Residual K



Relies on Linear Superposition of K's

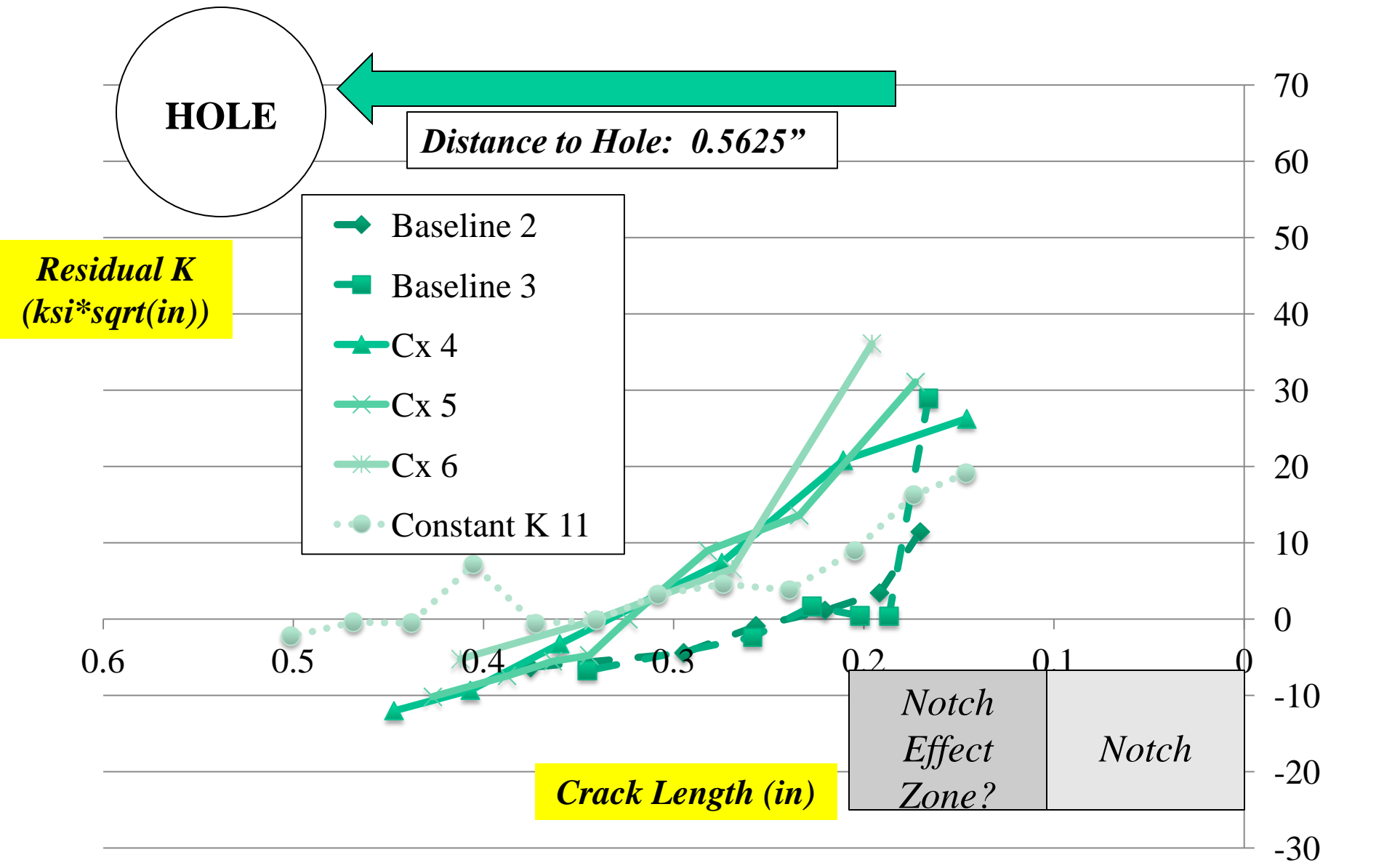


'Classic' Residual K Results



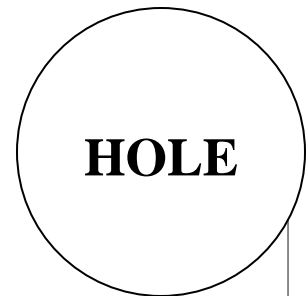


$e/d = 2.0$: *Same Data* Averaged for 5 Increments





'Classic' Residual Stress Results



Distance to Hole: 0.375"



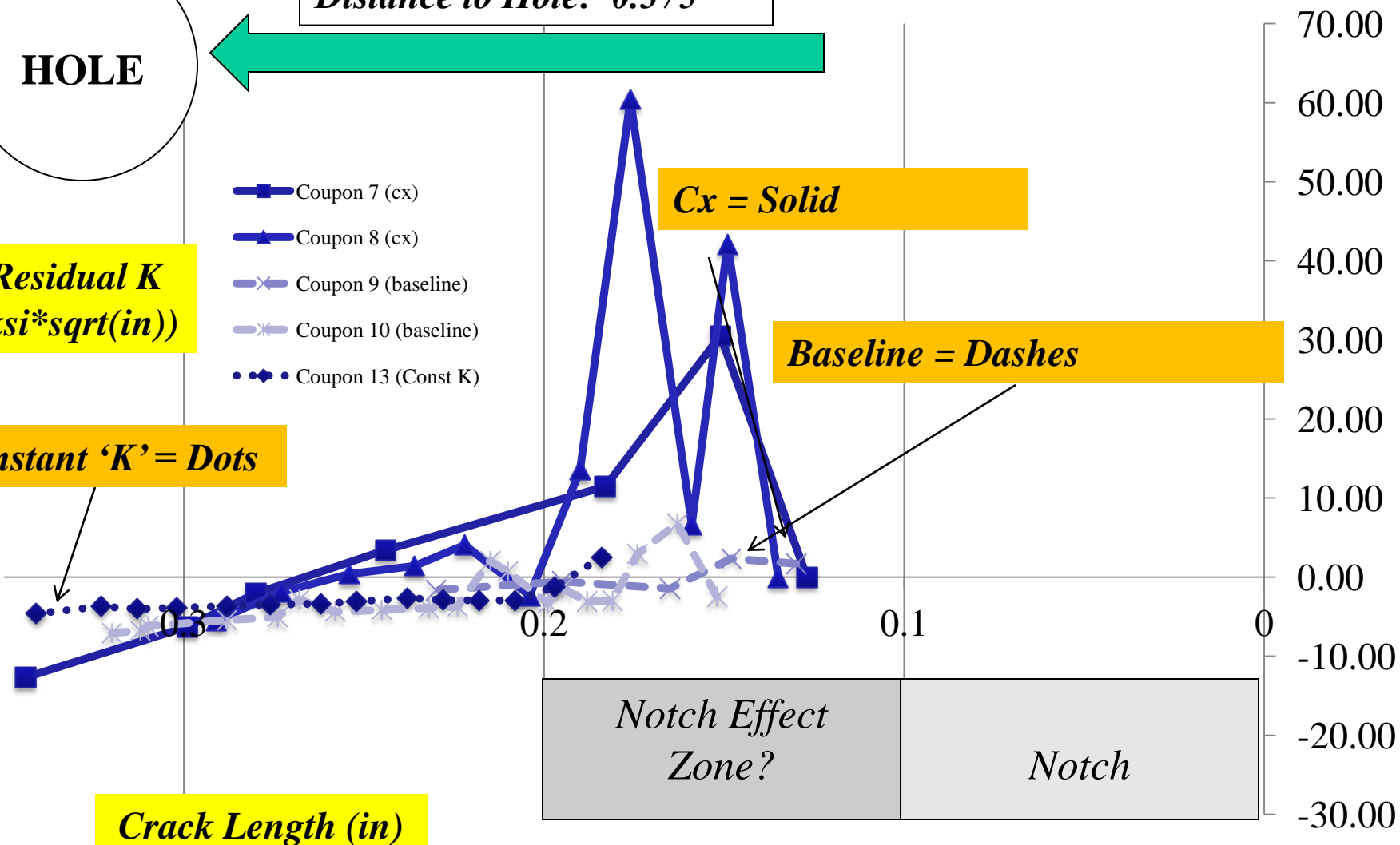
- Coupon 7 (cx)
- Coupon 8 (cx)
- Coupon 9 (baseline)
- Coupon 10 (baseline)
- Coupon 13 (Const K)

Residual K
(ksi*sqrt(in))

$Cx = Solid$

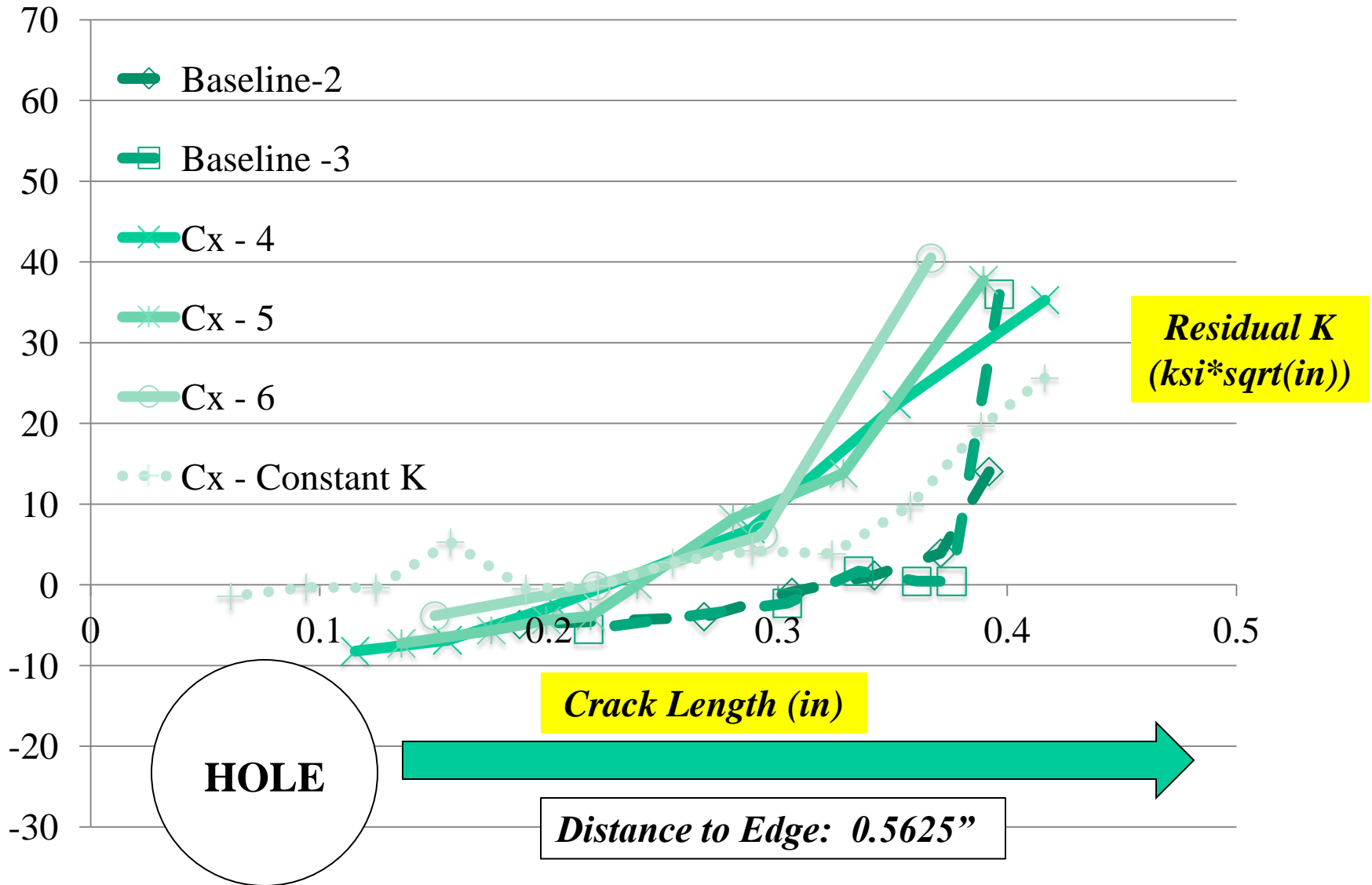
Baseline = Dashes

'Constant K ' = Dots



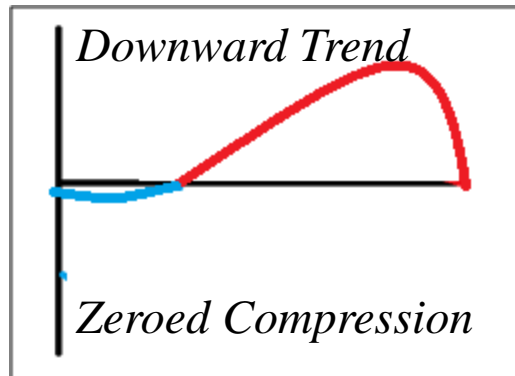
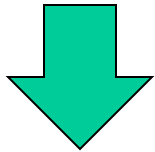
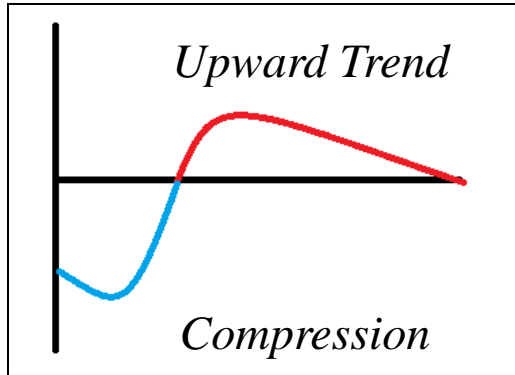


For Completion: *Forward Residual K Field*





Home Stretch



Conclusions

The compressive field is significantly reduced after the tensile field is cracked through

The total life of the coupons was unchanged by cold working with the crack growing in the continuing damage scenario

Huge variability is present in the tensile region of the residual stress field, but is most likely caused by the notching of a cold-worked specimen

Constant K results point to stress dependencies in the residual stress field (further replicates required)



Suggestions for Future Work:

Things you may or may not want to do



- Use the tensile residual stress field to predict the compressive residual stress field
 - Can you destroy it in enough ways to assemble a residual stress profile?
- Testing the residual stress superposition technique:
 - Does a spectrum dependency occur?
- Equating FOD to residual stress
 - Do you always see a significant variability in Kres?
- Other usual suspects
 - More holes, thicker plates, larger plates, material misorientation, mishapen/square holes, front and back side cold-working

“Interest does not always equate to time.”

-Ted Nicholas



Done.





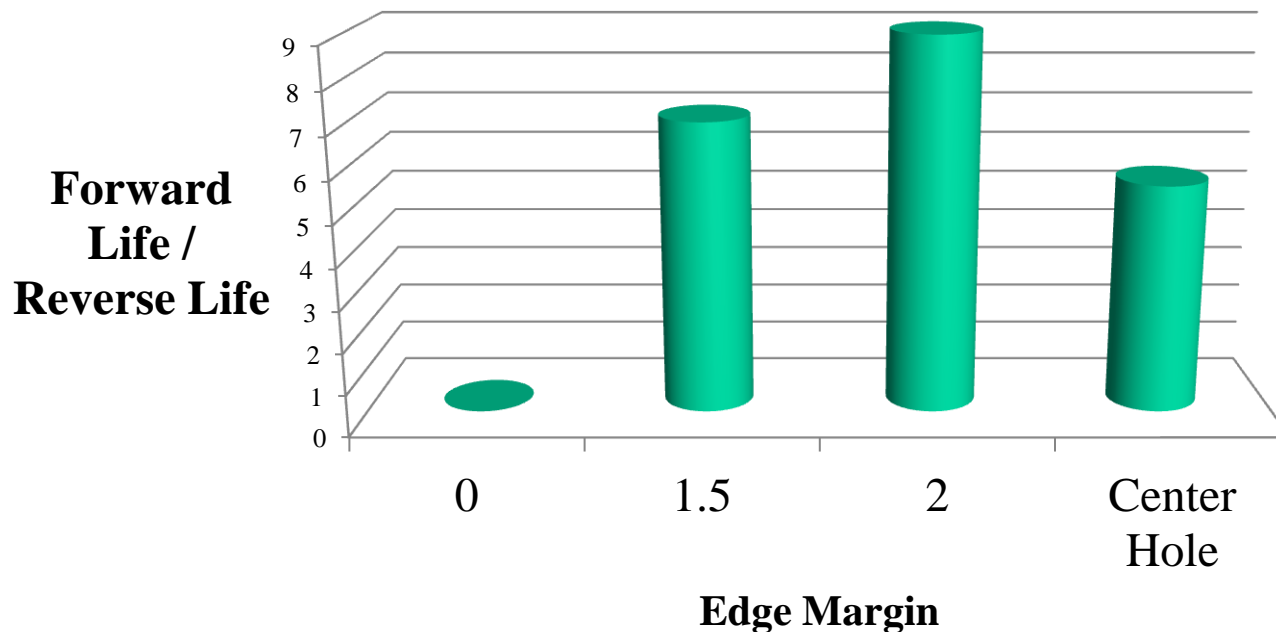
Backup Slides



A Quick Look at the Geometry

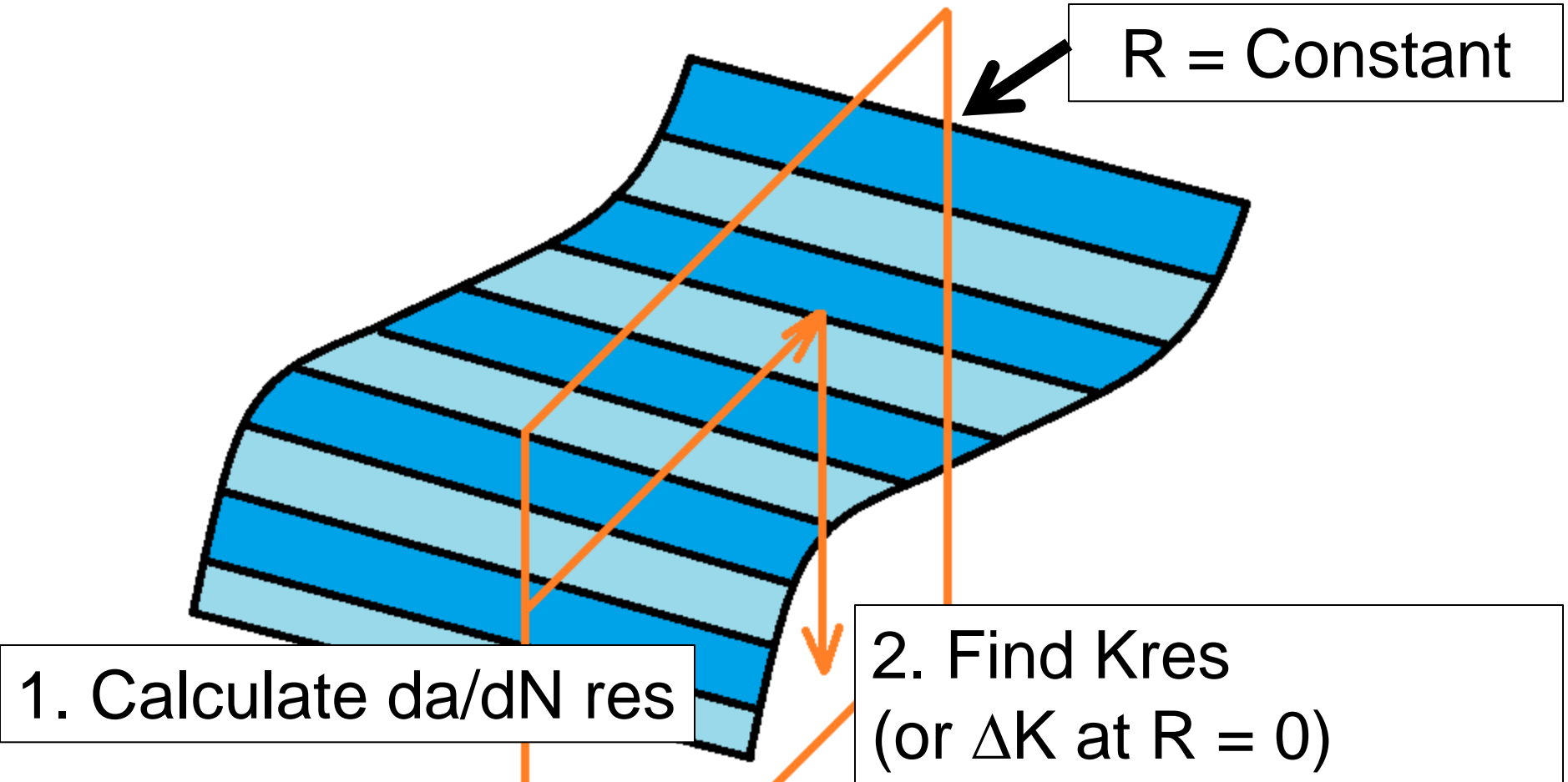


- What edge margin gives the most significant jump in fatigue life?
 - 15 ksi, $R = 0.0$, Constant Amplitude
 - 0.05” Through Crack





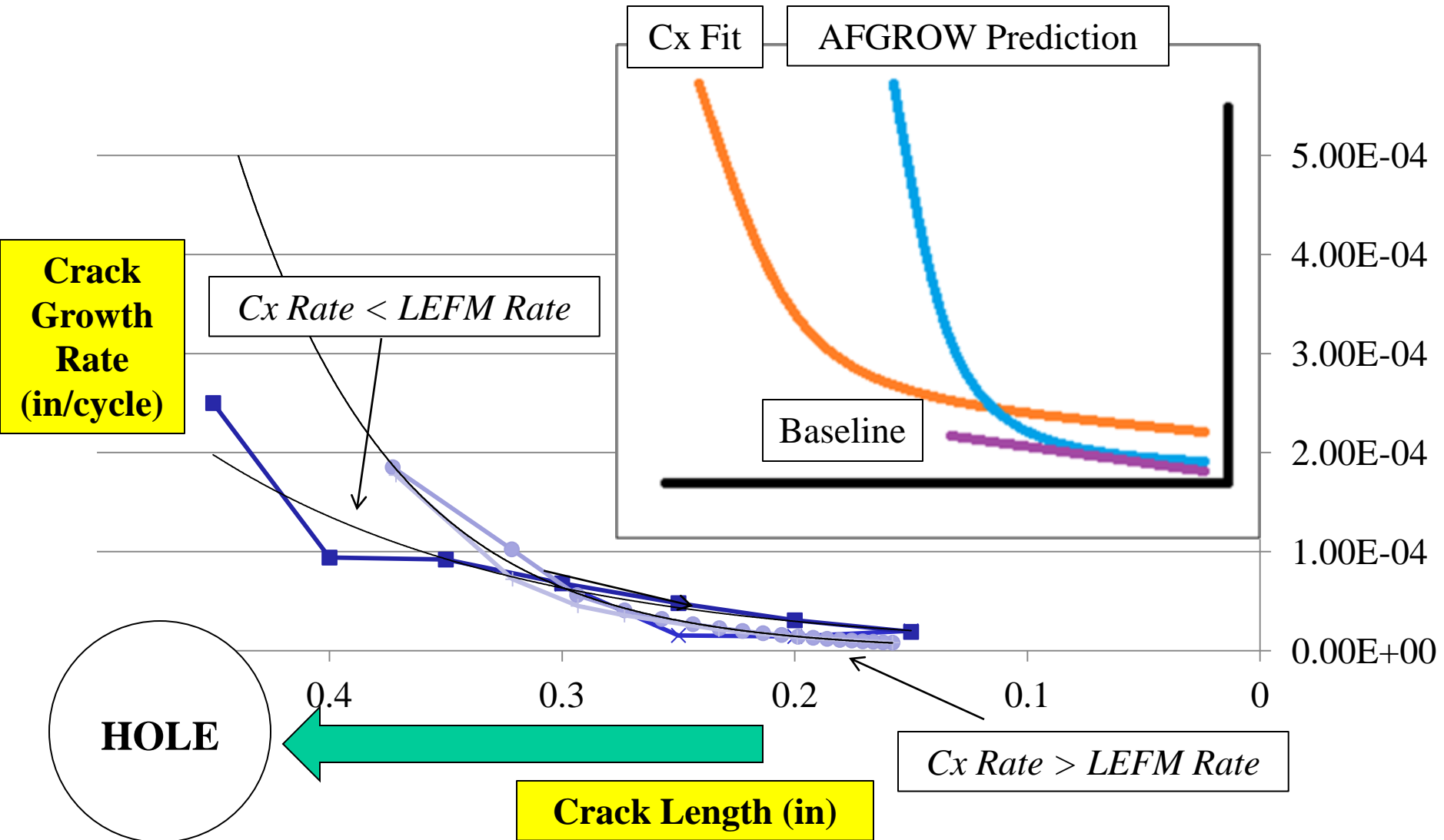
'Subtraction' Method



Assumes FCG Curve is applicable to K_{res} and velocities are superimposed



Subtraction Method: A Look at the Growth Rate Behavior



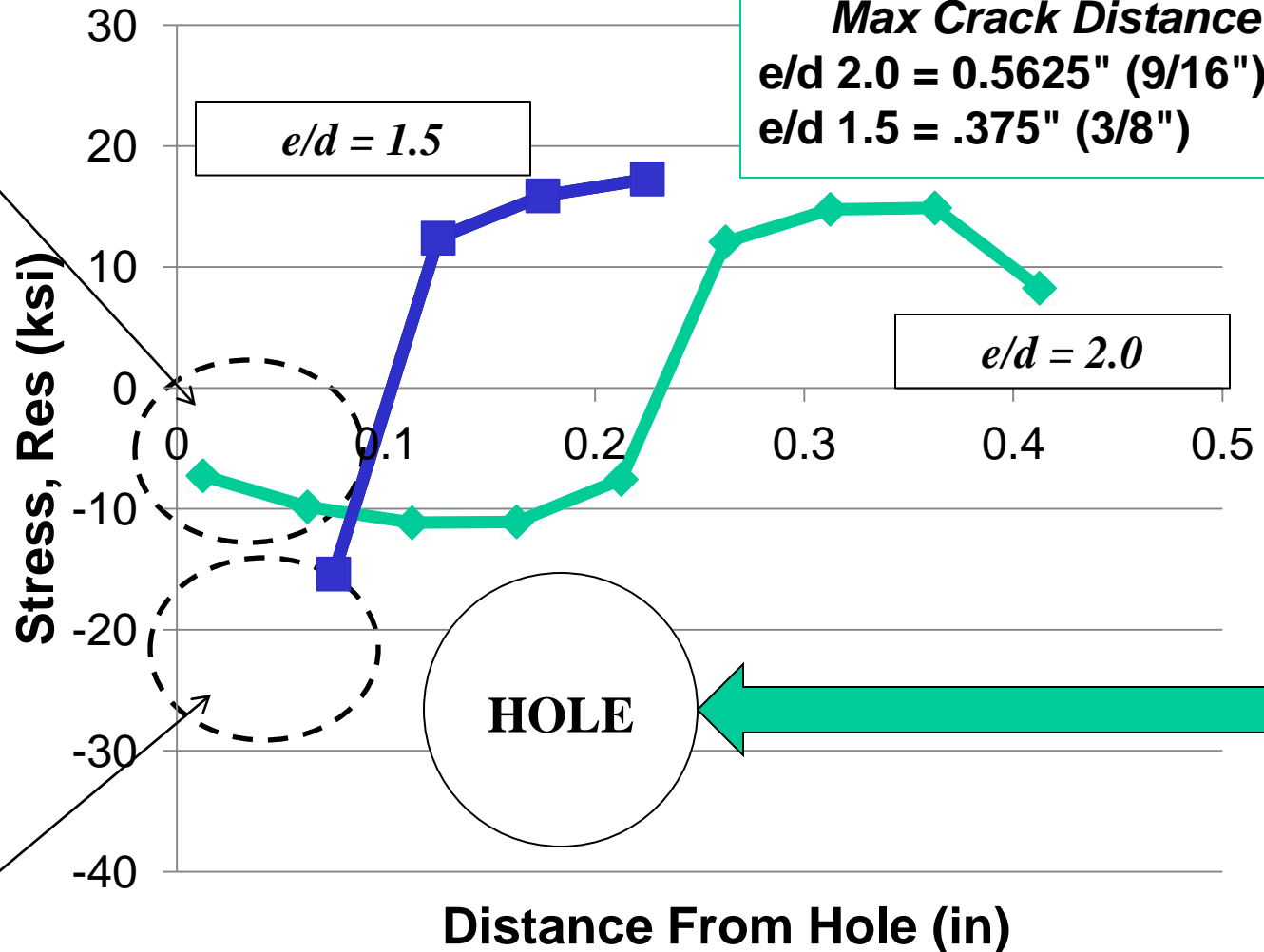


Subtraction Method

σ (res)



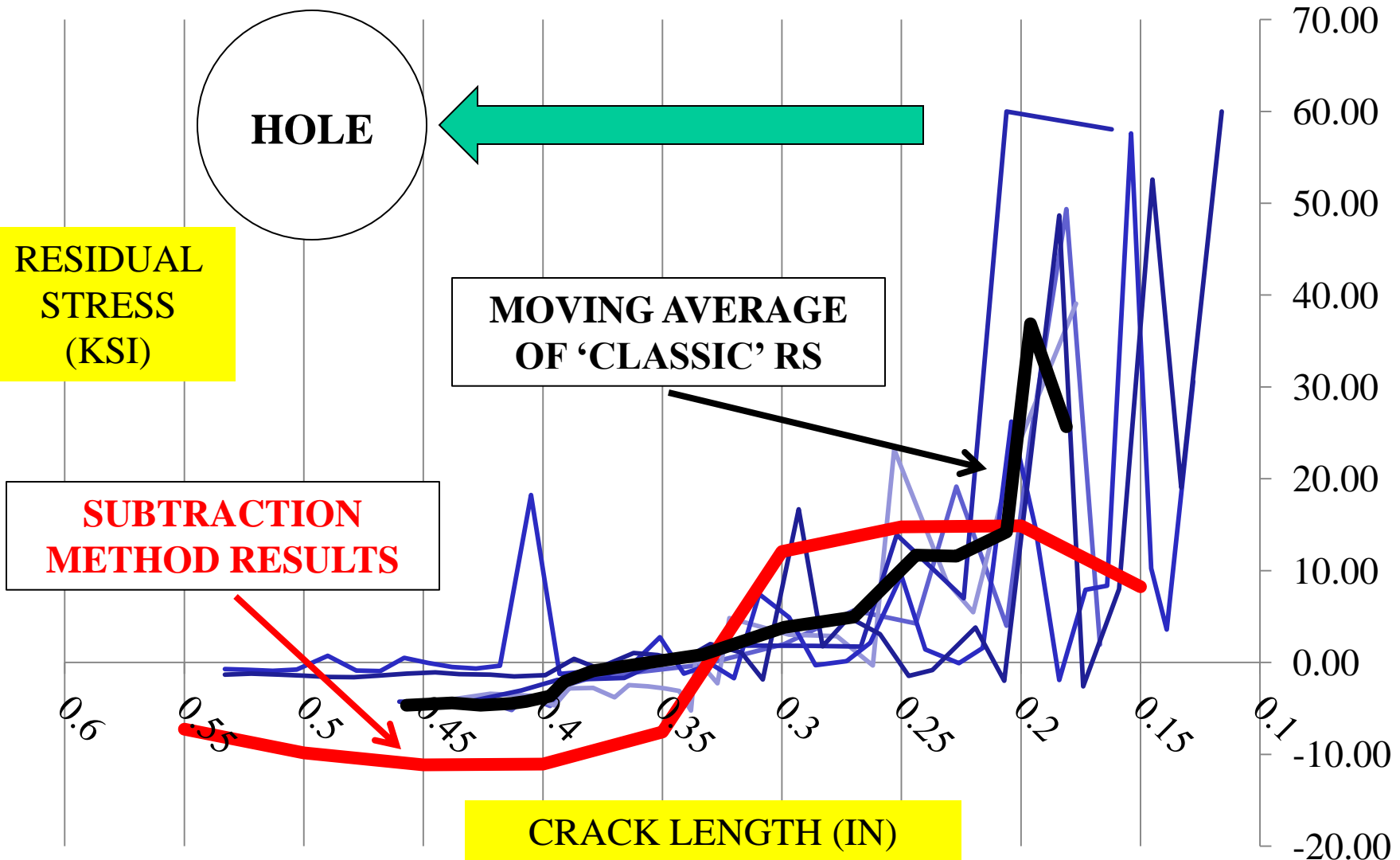
*Increased
Sampling Rate
to Acquire More
Points Near
Edge*



*Higher
Localized
Stresses Made
Measurement
More Difficult*



Residual Stress Plot Overlay of $e/d = 2.0$



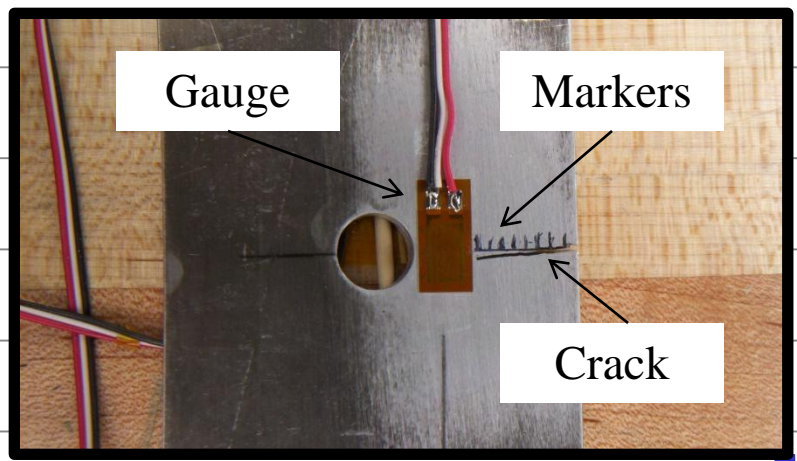
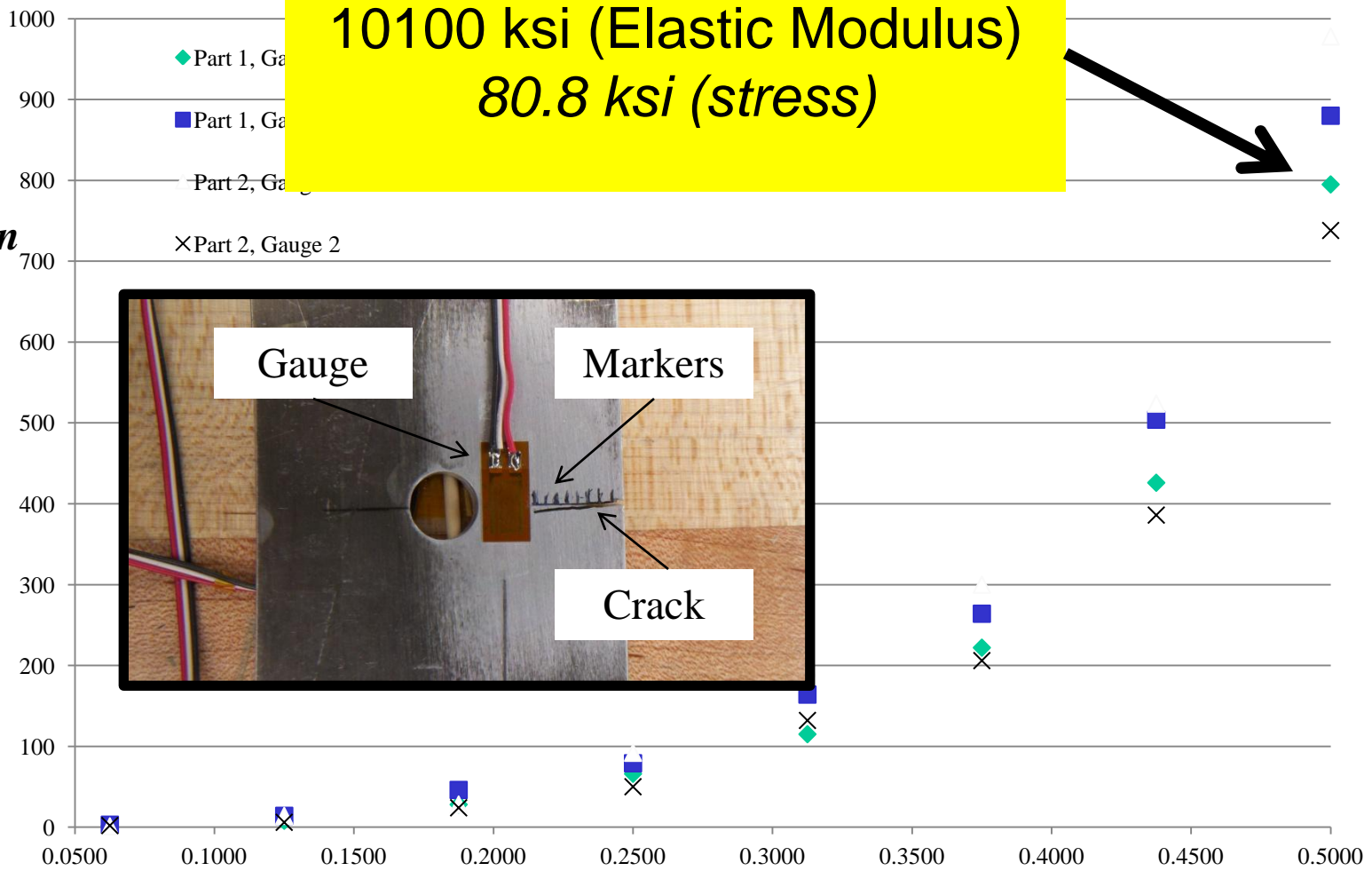


Which method is more right? ... checking the strain relief



800 $\mu\epsilon$ (strain)
10100 ksi (Elastic Modulus)
80.8 ksi (stress)

Microstrain



Crack Length (in)



How is each method implemented in a prediction?

**Classic:
Residual 'K' vs. 'c'
profile during LEFM run**



*Similitude
allows for a
master curve*

$$R = (K_{min} \pm K_{res}) / (K_{max} \pm K_{res})$$

**Subtraction:
Residual
'da/dN' vs 'c'
table**



*Tables will need
to be developed
for differing load
scenarios*

$$da/dN = da/dN (LEFM) + da/dN (res)$$



Background: The Rational to Reverse



- Forward Cracking
 - Low-load threshold (= Load Bumping)
 - ‘Strange’ crack shapes
 - Tensile field erasure
- Reverse Cracking
 - Peak compression not interfered by notch
 - Free to run any loading condition to get growth
 - Tensile effect is present

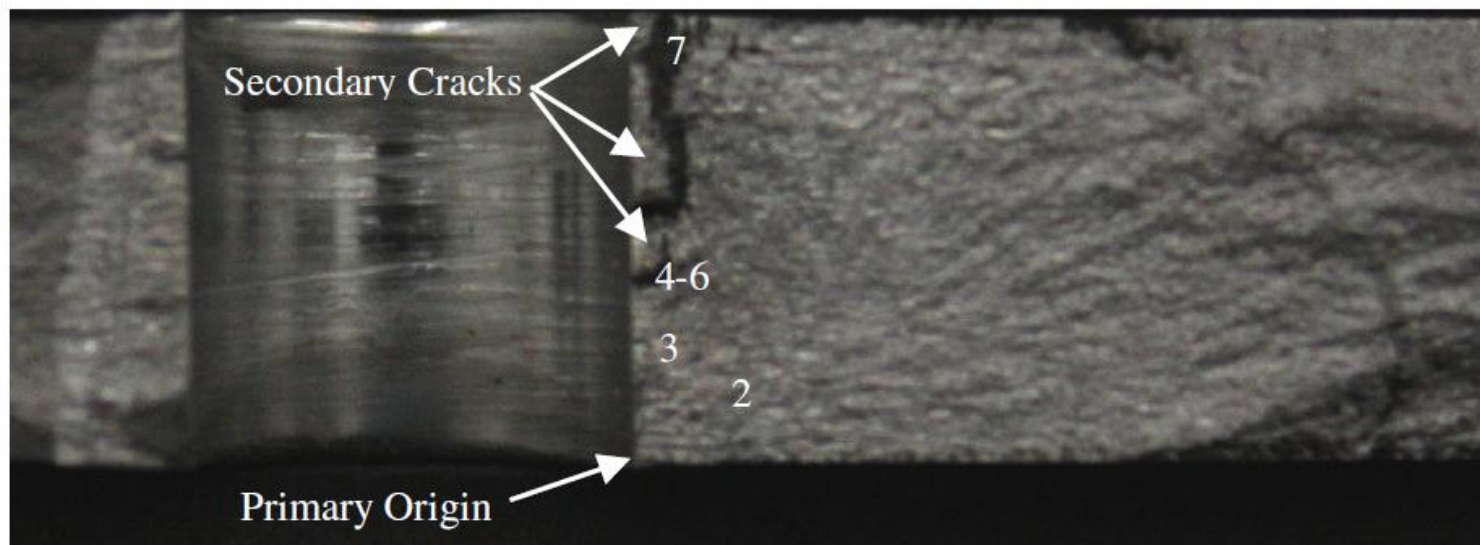


Figure 1. Coupon CX07 (AKA 1D07) Optical macro fracture view of specimen CX-07. Numbers indicate regions where subsequent images were taken using SEM.



Constant Amplitude Results: 15 ksi, R = 0, 2024-T3 (Al-Clad)



Life between $c = 0.15''$ and Failure at the Hole:

Pre-crack = 15 ksi

$$N_{Cx} > N_{\text{baseline}} \quad ; N_{Cx, 2.0} > N_{Cx, 1.5} \quad ; N_{\text{baseline}, 2.0} > N_{\text{baseline}, 1.5}$$

Total Life: $N_{Cx, 2.0} = N_{\text{baseline}, 2.0} = N_{Cx, 1.5} = N_{\text{baseline}, 1.5}$ (approx)

TEST MATRIX

R = 0.0

All loads in kips!

<u>Trial</u>	<u>Description</u>	<u>e/D</u>	<u>σ (ksi)</u>	<u>Pmax</u>	<u>Pmid</u>	<u>Pamp</u>	<u>Cycles to To .15"</u>	<u>Right Cycles to Failure</u>	<u>Left Cycles to Failure</u>	<u>Total Cycles to Failure</u>
1	Test Dummy	2.0	24	6	3	3				
2	Baseline	2.0	15	3.75	1.875	1.875	12000	9200	DNR	21200
3	Baseline	2.0	15	3.75	1.875	1.875	9500	12500	14000	36000
4	Cx	2.0	15	3.75	1.875	1.875	10500	6750	12810	30060
5	Cx	2.0	15	3.75	1.875	1.875	11000	6550	11908	29458
6	Cx	2.0	15	3.75	1.875	1.875	12700	4950	11766	29416
7	Cx	1.5	15	3.75	1.875	1.875	8000	2500	19535	30035
8	Cx	1.5	15	3.75	1.875	1.875	5500	2700	13525	21725
9	Baseline	1.5	15	3.75	1.875	1.875	14500	3500	8233	26233
10	Baseline	1.5	15	3.75	1.875	1.875	12500	4800	11459	28759



Test Matrix: FYI



<u>Trial</u>	<u>Description</u>	<u>e/D</u>	<u>σ (ksi)</u>
1	Casualty	2.0	24
2	Baseline	2.0	15
3	Baseline	2.0	15
4	Cx	2.0	15
5	Cx	2.0	15
6	Cx	2.0	15
7	Cx	1.5	15
8	Cx	1.5	15
9	Baseline	1.5	15
10	Baseline	1.5	15
11	Cx (Const K)	2.0	15
12	Cx (Const K)	2.0	15
13	Cx (Const K)	1.5	15
14	Cx (Const K)	1.5	15
15	Center Hole(IP)	2.67	15
16	Center Hole(IP)	2.67	15
17	Forward (Const K)	1.5	15
18	Forward (Const K)	2.0	15
19	Forward (Const K)	2.0	15



Background: The Rational to Reverse

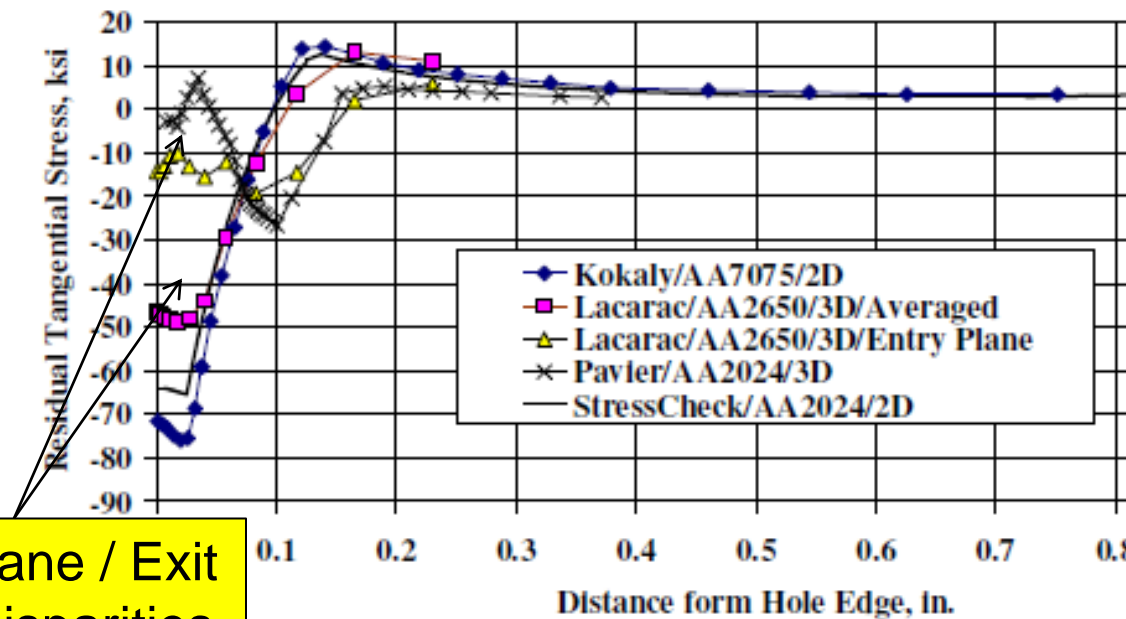


- *Back-Cracking*
 - Another perspective on Cx holes
 - Peak of the R.S. field will not be interfered by notch
 - Tensile effect is fully present
 - Free to run at any operational load
 - The Intangibles
- *Downsides*
 - The test gets exciting at the peak of the R.S. compressive zone
 - Flipping Sigma (Res) to calculate K (Res) / tensile relief may be problematic
 - Elastic response will change residual stress field*



The Motivation

How do you account for the fatigue life benefit of a cold worked hole?



Small Displacements & Unknown Material Properties Create a Measurement Nightmare for Stress Fields!

Entry Plane / Exit Plane Disparities Make a Conclusive RS Field

Fatigue Crack Growth Models Compound Your Problems!

Comparison of Finite Element Simulations from S



Method #2: Subtraction

$$da/dN_{res} = da/dN_{test} - da/dN_{LEFM/baseline}$$

$$K_{res,backward} (da/dN_{res}, \mathbf{R(LEFM)} = \mathbf{0})$$

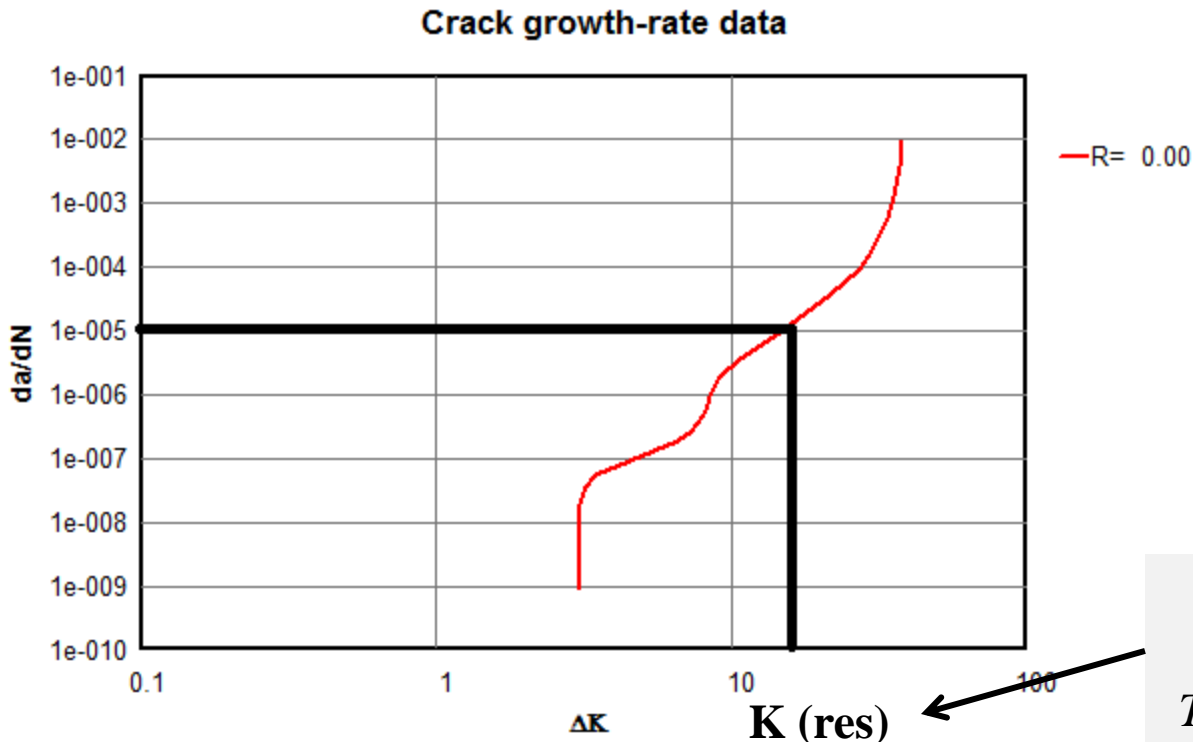
$$\sigma_{res} (K_{res,backward}, \beta_{backward}, a)$$

$$K_{res,forward} (\sigma_{res}, \beta_{forward}, a)$$

Why?
Based on direct
measurement

Superimposes
Velocities...
i.e...
Conservation of
Momentum

da/dN (res)



Assumes:
 $dK = K_{res} - 0$
Thus: Use $R = 0$

Note: For $R < 0.0$, K_{max} is used instead of Delta K



Method #1: K_{res} 'Classic' in 2D

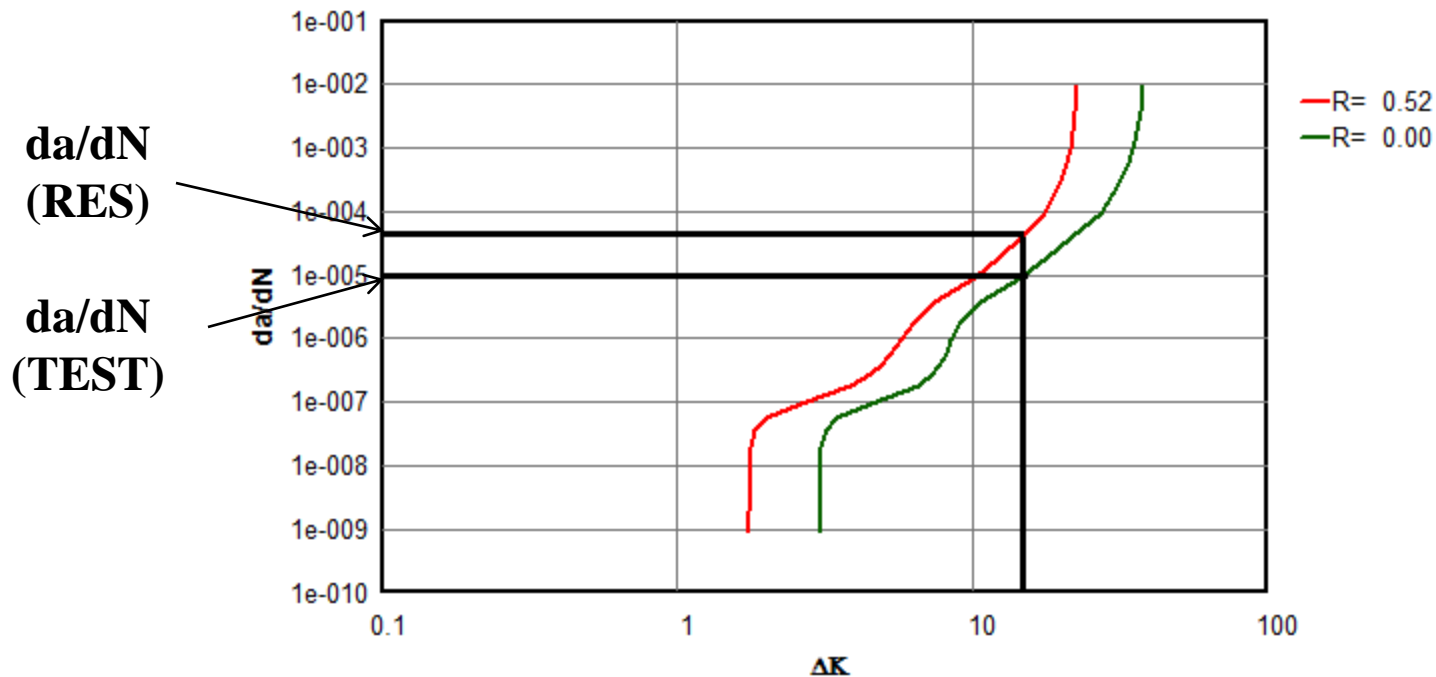
$$R_{res} (\Delta K, da/dN_{test}) \rightarrow K_{res,backward}(R_{res})$$

$$\text{Where: } R_{res} = (K_{min} + K_{res}) / (K_{max} + K_{res})$$

$$\sigma_{res} (K_{res,backward}, \beta_{backward}, a)$$

$$K_{res,forward} (\sigma_{res}, \beta_{forward}, a)$$

Crack growth-rate data

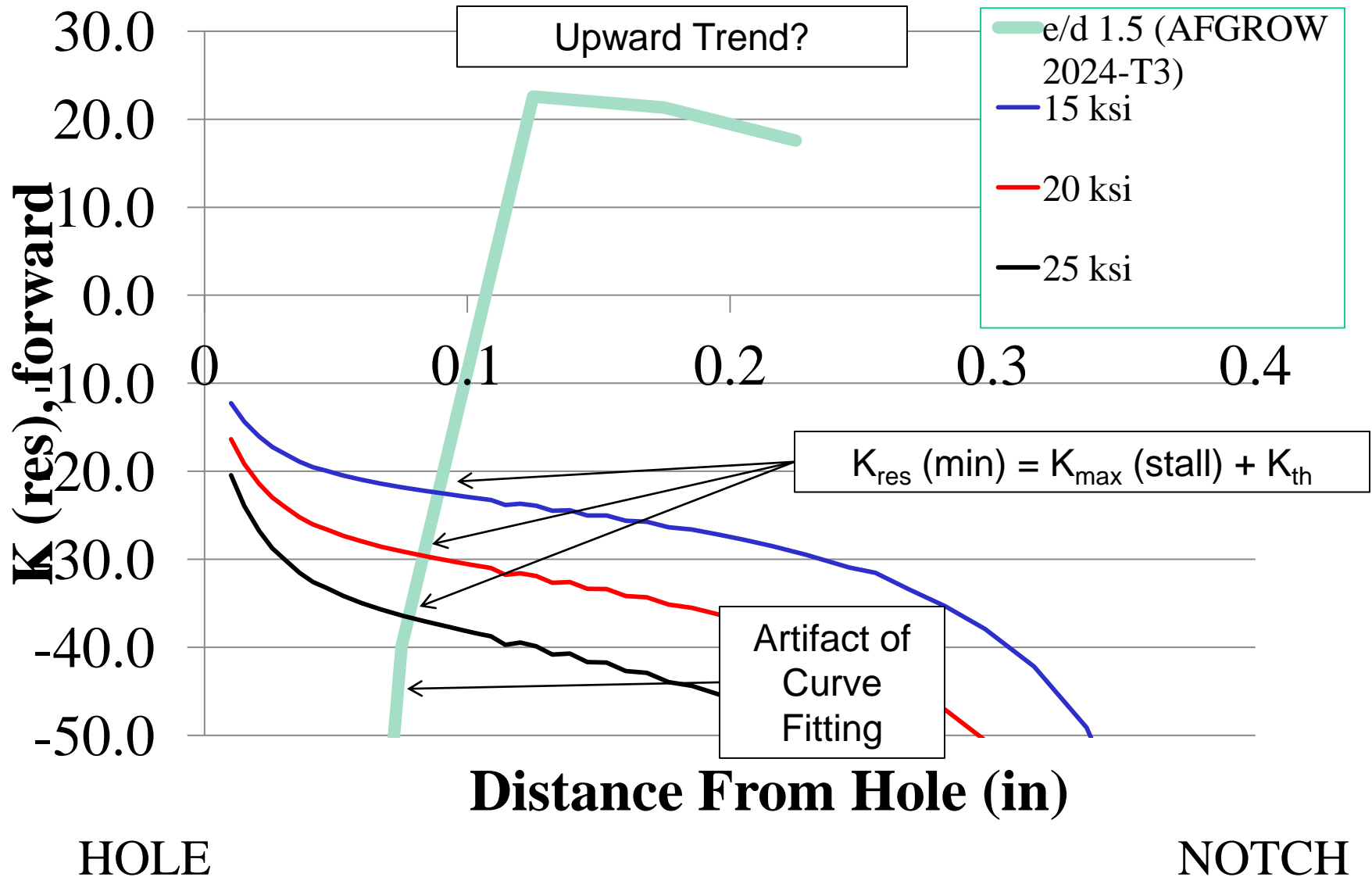


Note: For $R < 0.0$, K_{max} is used instead of ΔK



Inversion of the Residual Stress Field

$K(\text{res})$ for $e/d = 1.5$





Inversion of the Residual Stress Field

$K(\text{res})$ for $e/d = 2.0$

